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A Maude-Based Formal Approach to Control and Analyze Time-Resource Aware Missioned Systemsof-Systems

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Abstract— Systems-of-Systems (SoSs) are increasingly utilized to integrate multiple Constituent-Systems (CSs) and fulfill missions surpassing the capabilities of individual systems. Successful mission execution relies on effective management of time and resources. Time constraints denote the timeframes within these missions must be completed, and resource constraints involve the allocation of necessary resources for execution. Addressing these dynamic behavior factors in SoSs poses significant challenges and necessitates the adoption of control strategies for efficient coordination and execution of missions. To confront these challenges, this paper introduces a novel hybrid approach, merging an MDA technique (TRC-MM: Time-Resource Aware Control Meta-model) and Maude language to formally specify and control missions. This approach specifically incorporates time-resource aware missions, resource dependencies, and control mechanisms in the dedicated TRC-MM. Further, RT-Maude is utilized as the formal specification language to develop an executable formal model for the controller's behavior in SoSs' missions, offering a powerful analysis method to express and verify behavioral properties pertaining to time and resource constraints.

Keywords—SoS, Maude, Formal Method, Model-checking, Timed mission, Control strategies.

I. INTRODUCTION

Systems-of-Systems (SoSs) have emerged as a prominent solution to tackle the challenges posed by large-scale integration and coordination of IT systems. SoSs involve the seamless integration and execution of multiple Constituent-Systems (CSs) to achieve missions that individual CSs cannot accomplish alone [1]. The centralized control in these systems ensures a cohesive and coordinated approach towards the common goals of SoSs. The presence of a central authority enables effective management, coordination, and alignment of the CSs' towards the common goals of the system [1] [2].

Designing SoSs to address centralized control challenges and ensure adherence to specified behavior is complex. This process includes selecting the optimal functional chain to achieve overall missions at the SoS level within time constraints and implementing effective strategies, regulatory mechanisms, and corrective actions at the CSs level. Developing a corresponding formal model is also crucial to analyze, simulate, and verify logical properties. To this end, this paper proposes a systematic approach using a metamodel, TRC-MM, designed to optimally arrange CSs to fulfill mission objectives within time and resource constraints. TRCspecifically addresses time aspects, dependencies, and control mechanisms, allowing for dynamic adjustment of behavior to changing runtime conditions.

Fig.1 describes the three main steps of our approach. Firstly, it starts by introducing a generic TRC-MM that captures the essential structural, behavioral, and quantitative

aspects. The *TRC-MM* serves as a support tool that enables the creation of concrete models tailored to specific application domains within SoSs. The adopted MDA technique ensures a comprehensive representation of characteristics, including temporal aspects and resource allocation. Secondly, we rely on a formal execution semantic using a rewriting engine based on RT-Maude and Strategy Language [3] [4] to control and simulate the dynamic behavior of the proposed controller. Lastly, we use model-checking tool of RT-Maude to verify the satisfaction of some specific properties and constraints.

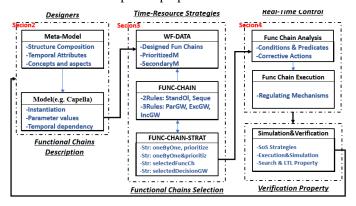


Fig. 1. The proposed approach.

II. MODELING TIME-RESOURCE AWARE MISSIONS IN SOS

This section focuses on creating the *TRC-MM*, specifically designed for Time-Resource Aware Missions in SoSs.

A. TRC-MM: Time-Resource Aware Control Meta Model

The TRC-MM serves as a standardized set of basic classes that capture the essential aspects of missioned SoSs. It integrates into a systematic framework, encompassing structural, behavioral, control strategies, etc. In Part1 of Fig. 2, we find classes that represent specific missions within the CSs. They are associated with MTemporalConstraints and States classes that capture the various states of a given mission. Readers are referred to [2] for more details. Part2: represents the entities or components required for executing missions within the SoS. It is associated with ResourceStates with PrvRes and PubRes for private and global resources that describe the various states, types or categories of resources. The ResPool class represents a centralized repository or pool of resources that can be shared and allocated among missions in the SoS. In the controlled time bound missions, the ResPool serves as a shared repository for spare or unused resources within CSs. When a CS has surplus or available resources that are not currently being utilized, it contributes those resources to the Resource Pool, allowing other CSs to

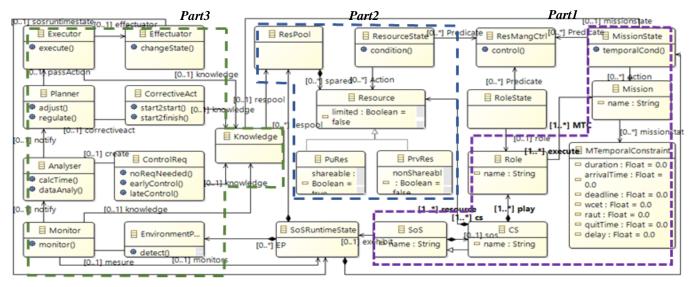


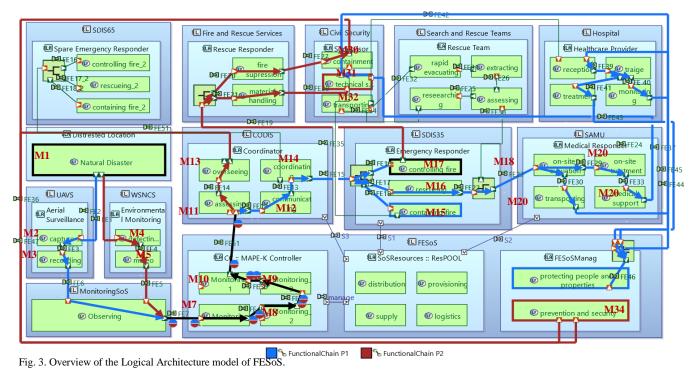
Fig. 2. Time-Resource Aware Control Meta-Model for SoS.

utilize them. *Part3* represents classes that are associated with *MissionState* and *ResPool*, serving as the knowledge base that stores information about the current state of missions and the availability of resources.

B. Running Example: French Emergency SoS

The case study highlights the logical architecture design of the French Emergency SoS [7] [8]. The deduced model of FESoS is based on *TRC-MM* and its logical architecture is designed using Capella editor [18] as show in Fig. 3. The FESoS is designed for emergency protection, it features interconnected CSs and missions such as MonitoringSoS deploying UAVs¹ and WSNCS², CODIS³ overseeing operations, and SAMU⁴ for emergency medical services. The HospitalCS manages patient reception and assessment, while medical treatments

and continuous monitoring are ensured. Civil Security is crucial for coordination, ensuring information flow and collaboration. SDIS64⁵ and SDIS65 represent firefighting efforts of two departments, deploying equipment and firefighters. Search and Rescue Teams prioritize finding and evacuating survivors, while the Fire and Rescue Services handle fire control and hazardous materials. The study underscores the integrated efforts of these CSs to safeguard people and property. The FESoS model focuses on the representation of multiple alternative paths or simultaneous missions' execution. In addition, parameter values offer a comprehensive insight into the functional chains, aiding designers in exploring and assessing various design options and system behaviors, Fig. 4 capture a piece of the entire figure which shows the description of the functional chains of the FESoS behavior.



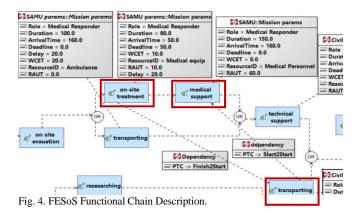
¹ Unmanned Aerial Vehicles

² Wireless Sensor Net

³ Centre Opérationnel Départemental d'Incendie et de secours

⁴ Service d'aide médicale urgente

⁵ Service Départemental d'Incendie et de Secours



III. MAUDE-BASED FORMAL SPECIFICATION OF SOSS CONTROL

This section presents the specification of dynamic SoS control mechanisms, emphasizing the SoS's global-level controller, with the objective of optimizing functional chain execution for efficient global mission attainment. Simultaneously, at the mission and local CSs levels, the controller oversees RT-regulation to reduce execution time.

A. RT-Maude and Strategy Language

By leveraging Maude's concurrent rewriting capabilities and equational structural axioms, we can logically deduce and reason about the behavior of the system[4]. In the context of temporal mission priorities and states, the modules in RT-Maude denoted as a tuple $R = (\Sigma, E \cup A, R)$ provide a formal and structured representation of the system's behavior and transitions, incorporating temporal aspects. The equational theory part of the modules, represented by $(\Sigma, E \cup A)$, encompasses the signature $\Sigma = (S, C, \leq, F, M)$, which includes sorts and subsorts S, class names C, a subclass relation \leq , and a set of functions and messages. The set E denotes equations and membership tests, some of which can be conditional, while A represents equational axioms associated with specific operators in the signature Σ . The tuple R consists of both conditional and nonconditional rewrite rules. In the context of Real-Time rewriting theory, $(\Sigma, E \cup A)$ includes an additional sub-theory ($\Sigma TIME$, $\Sigma TIME$) \subseteq (Σ , E \cup A), specifically modeling time. The behavioral transitions are defined using rewrite rules of the form: crl[R]: $\{t\} => \{t'\}$ in time u if (condition). Using these rules, we can accurately model how time and the states of the system evolve, which is crucial for understanding and verifying the properties of RT and hybrid systems. RT-Maude extension is designed to decouple the rewrite rules, from their execution via strategies. The system module's definition evolves into $(\Sigma, E \cup A, S(R, SM))$, where S characterizes the system's behavior. i.e. S is delineated by two components: R, which comprises a set of potential conditional rewrite rules, and SM, the strategy module directing the rewriting procedure. Rewrite rules define transitions between the configurations. RT-Maude' high-performance rewrite engine, allows simulation, analysis, and model-checking. Maude offers commands to explore system behaviors from an initial configuration, e.g. rewrite, srewrite, and tsearch.

B. Maude-based Specification of TRC-MM Static Entities

The *TRC-MM* entities can be mapped to a set of RT-Maude concepts. Table.1 summarizes the operational semantic of different static elements introduced in *TRC-MM*, i.e. we enumerate all sorts and operators essential for characterizing SoS. The primary classes defined are *SoS*, *CS*, and *Mission* accompanied by their associated sorts and ops.

TABLE 1: RT-MAUDE SEMANTICS OF THE TRC-MM's ELEMENTS.

Entities	RT-Maude specification				
SoS	class SoS clock : Time, CSsSet : CSIdSet, , missionSet : GMIdSet				
CS	class CS clock : Time, missionSet : MIdSet .				
Mission	class Mission localClock : Time, duration : Time, arrivalTime :				
Role	Time, quitTime: Time, delay: Time, deadline: Time,				
	$mission State: Mission State\ res Type: Res Type, RAUT: Time\ .$				
	class Resource localClock : Time, resType : ResType,				
CSs Queue	sort CSIdSet .				
	subsort Oid < CSIdSet .				
	subsort Oid < MIdSet < GMIdSet .				
resPool	subsort Resource < ResourcePool .				
MissionState	ops arrived accomplished pending failed : -> MissionState .				
ResType	ops shareable nonShareable limited renewable: -> ResType				
ResState	op resType:_resState:_quantity:_ : ResType State Time ->				
Pool	Resource [ctor] .				
	op emptyPool : -> ResourcePool [ctor] .				
	op '[Pool:_'] : ResourcePool -> ResPool [ctor] .				
	op indeterminatedWF : funcChain -> Bool .				
Conditions	eq calcState(DD, ED, DT) = if (DD $>$ ED plus DT) then				
	accomplished else pending fi . eq calcQuitTime(ED, DT)				
	eq calcQuitTime(ED, DT, ST) = ED plus DT plus ST.				
	eq calcRemainedResource(ST, D) = ST plus D.				
	eq indeterminatedWF(M2 M3 SecondoryM PrioritizedM M1)				
	eq indeterminatedWF(M1 M2 SecondoryM PrioritizedM)				
Corrective	msg initSoS : Oid -> Msg .				
actions	msg finishAt : Oid Time -> Msg .				
	msg start2Start : Oid -> Msg .				
	msg start2Finish : Oid Time -> Msg .				
	msg finish2Start : Oid Time -> Msg .				

C. Control Strategies Formal Semantics

In this section, we propose strategies for optimal functional chain or mission's workflow selection, exploring their role in efficient global mission attainment by minimizing execution time and optimizing resources. Table 2 aligns each behavioral element of the *TRC-MM* with semantics, specifying the mission's workflow in three Maude modules:

(1) WF-DATA module: along with two other constants: PrioritizedM represents a subset of missions that are given priority in terms of short duration and resource constraints, and SecondaryM denotes missions that are not prioritized for scenario but still exist within the SoS and could be relevant in future executions. The operator "Union" denoted by _|_ signifies the classification of missions designating the secondary and prioritized missions that will be selected to execute in the functional chain. The conditions specified in the indeterminatedWF (Table. 1) outline the predicates under which certain mission workflows (caused by gateways) are in a nondeterminate states, making it challenging to predict or control the exact sequence of missions for optimal outcomes.

TABLE 2: MISSION PRIORITIZATION AND MANAGEMENT

Rule	Condition	Action	Description	
standaloneM (M1)	M1 without any order		A single mission M1, is promoted to the prioritized list.	
sequenced (M1,M2)	M1, M2 Are sequenced		M1 and M2 are sequenced and both are promoted to the prioritized list.	
parallelM- GW(M1,M2)	M1, M2 are in parallel	,	M1 and M2 are concurrently promoted to the prioritized list.	
GW(M1, M2) / inclusiveM-	Duration(M1) < Duration(M2) OR RAUT(M1) < RAUT(M2)	PrioritizedM	M1 is prioritized if it completes faster or uses resources more efficiently; otherwise, if neither condition is met, M1 is prioritized based on its shorter duration	

(2) FUNC-CHAIN module: it imports the previous module and it involves the possible executions of missions specified using rewriting rules (see Table 2). The first two rules are implemented to execute standalone and sequence missions, the other three rules are specified to execute the branching and merging nondeterministic behavior introduced by gateways(parallelM-GW, exclusiveM-GW and inclusiveM-

GW). These gateways might not always result in the most efficient execution because there are situations where the workflow can become indeterminate when using gateways.

(3) CHAIN-STRAT module: It tackles the challenge of managing nondeterminism states in mission execution. To achieve this, we enforce strict control over gateway rules before initiating standalone and sequenced execution rules. This enforcement is accomplished through the specification of a set of strategies within this module. The strategy *oneByOne* applies either of the two execution rules (standaloneM or sequencedM), and the strategy prioritize applies any of the three gateway rules. The strategy oneByOne&prioritize applies either of two previous strategies based on the rules of FUNC-CHAIN, executing only if prioritize isn't an option. The selectedFuncCh strategy is recursive, continually repeating this process until the global mission is achieved. Meanwhile, *selectedDecisionGW* strategy is more selective, focusing on the outgoing branches (i.e., prioritized missions) and sidestepping all secondary mission paths. Example:

sd selectedDecisionGW := (match SecondoryM | PrioritizedM M1 M2 M3) ?
idle : (oneByOne&prioritize ; selectedDecisionGW) .
sd selectedFuncCh := (match SecondoryM | G) ? idle : (oneByOne ;
prioritize ; selectedFuncCh) .

D. Local Control Mechanisms of Missions

We present in this section a formal specification of the self-regulating of the SoS controller; it allows to monitor locally the functional chain execution, analyze temporal attributes and execute corrective actions adjusting missions of a given CS to guarantee timely completion. See Table 3.

TABLE 3: TEMPORAL CONTROL MECHANISMS FOR SoS MISSIONS

Conditions	Corrective Action	Description	
M1 arrives earlier than expected M1 arrives at time T	Start-2-Start (S2S) adjustment for M2 M2 starts at time T	Adjust the start time of M2 based on M1's arrival	
(T < T') M1 arrives earlier than expected	Start-2-Finish (S2F) adjustment for M2	Adjust the finish time of M2 based	
M1 arrives at time T (T < T ')	M2 finishes at time T	on M1's arrival	
M1 takes longer to complete	Finish-2-Start (F2S) adjustment for M2	Adjust the start time of M2 based	
T < than initially anticipated	M2 starts at time T	on M1's delay	
M1 takes longer to complete	Finish-2-Finish (F2F) adjustment for M2	Adjust the finish time of M2 based	
T > than initially anticipated	M2 finishes at time T	on M1's delay	
No deviations or issues	No corrective action required	missions are proceeding as planned	
	M1 arrives earlier than expected M1 arrives at time T (T < T') M1 arrives earlier than expected M1 arrives at time T (T < T') M1 takes longer to complete T < than initially anticipated M1 takes longer to complete T > than initially anticipated No deviations or	M1 arrives earlier than expected adjustment for M2 M1 arrives at time T (T < T') M1 arrives earlier than expected adjustment for M2 M1 arrives earlier Start-2-Finish (S2F) adjustment for M2 M1 arrives at time T (T < T') M1 takes longer to complete adjustment for M2 T < than initially anticipated M1 takes longer to complete adjustment for M2 T > than initially anticipated No deviations or No corrective action	

Conditions part in the table considers resource availability and time constraints. It utilizes equations to assess the accessibility of required resources within the specified constraints. Moreover, the specification leverages RTmessages and operations to implement corrective actions in table such as *start2start*, *ASAP*, etc. This generates Regulating Mechanisms that address these temporal constraints, manages execution and facilitates corrective actions in response to changing conditions using rules. Table 3. explores the temporal control mechanisms seen in TRC-MM, highlighting their relevance in addressing early arrival, late completion, and no control needed scenarios. In the case of Early Arrival, if Mission M1 arrives earlier than expected (at time T, where T < T'), the *Start-2-Start* (S2S) corrective action is applied. This adjustment ensures that Mission M2 starts at the same time (T) as Mission M1, synchronizing their execution. The table's entries illustrate the corrective actions for each control

mechanism, specifying the adjustments made to the starting and finishing times of the respective missions. These control mechanisms are related to the RT-Maude rules. For example, the *Start-2-Start* control mechanism can be represented as "crl[Start-2-Start]: {M1 starts at time T} => {M2 starts at time T} in time u if (T < T')". This rule signifies that if Mission M1 starts at time T and meets the condition of an early arrival (T < T'), then Mission M2 should also start at T.

```
rl [finish2start] : finish2start(M1, M2, ST) < M1 : Mission | loClock : D, duration : ED, arrivalTime : AT, quitTime : AT, delay : DT, deadline : DD, missionState : arrived, raut : RA > < M2 : Mission | loClock : D', duration : ED', arrivalTime : AT', quitTime : AT', delay : DT', deadline : DD', missionState : arrived, raut : RA > => < M1 : Mission | loClock : R, duration : ED, arrivalTime : ST plus R, quitTime : calcQuitTime(ED, DT, ST), delay : DT, deadline : DD, missionState : calcState(DD, ED, DT), raut : RA > < M2 : Mission | loClock : R, duration : ED', arrivalTime : calcQuitTime(ED, DT, ST), quitTime : calcQuitTime(ED, DT, ST) plus DT' plus ED', delay : DT', deadline : DD', missionState : arrived...
```

IV. VALIDATION THROUGH FESOS CASE STUDY

In this section, we aim to assess the controller's efficacy and verify model adherence to specific properties, focusing on Maude's model-checking and invariant. The approach involves a breadth-first search of states to confirm crucial SoS properties, validating invariants. If certain outcomes, the inverse of the invariant, are unattainable and the invariant is deemed true. If *search init* =>* C: Configuration such that not I(C:Configuration) yields no result, the invariant is valid.

A. Controlling FESoS with strategies

Fig. 3 illustrates various functional chains that have the potential to achieve global mission *M34*. These missions are designated as *M1*, *M2*, *M3*,...,*Mn* for simplicity. Using Maude Strategy Language, these specifications can be immediately executed. The 'search' command is particularly handy for this purpose, enabling exploration of all potential functional chain rules and identifying terms that correspond with a set target.

```
Maude> search initial =>* SecondoryM M1 M2 M3 M4 M5 M6 M7 M8 M9 M10 _| PrioritizedM . Solution 1 (state 54) states: 75 rewrites: 640 empty substitution No more solutions. states: 80
```

Even if the desired state can be achieved, there's always a certain degree of indeterminism regarding whether it adheres to the module's rules. Indeed, the path the *search* command followed to arrive at the global Mission M34 involves navigating through *indeterminatedWF* states. This can be validated by employing the *show path* command:

```
Maude> show path 10 .
state 0, M0: PrioritizedM | SecondoryM M1 M2 M3 M4 M5 M6 M7
===[ r1 ... [sequencedM] . ]===>
state 2, M1: SecondoryM M0 | PrioritizedM M2 M3 M4 M5 M6 M7
===[ r1 ... [sequencedM] . ]===>
state 10, M2: PrioritizedM M0 M1 | SecondoryM M3 M4 M5 M6 M7
```

Now, we can check whether the *M34* for instance can be reached by evaluating *selectedDecisionGW* from the initial state with the *srewrite* command. The answer is positive as shown in the following Maude code:

```
Maude> srew initial using selectedFuncCh .
Solution 1
rewrites: 74
result selectedFuncCh: SecondoryM | PrioritizedM M1 M2 M3 M3 M6 M7 M8 M9 M M10 M11 M12
M14 M16 M18 M20 M21 M31 M34
No more solutions.
rewrites: 74
```

B. Execution and Simulation

In FESoS model, missions *on-siteTreatment*, *transporting*, and *medicalSupport* are outlined, as visualized in Fig.5. These missions use specific resources, like *Ambulance* and *MedicalPersonnel*. The *on-siteTreatment* mission finishes before the other two missions which start simultaneously.

Designers, during the design phase, set parameters for each mission; for example, *on-siteTreatment* has a duration of 90 units, arrival time at 50 units, a delay of 20 units, and a resource usage time of 10 units. However, these inputs, grounded in available data and assumptions, don't fully factor in FESoS's dynamic nature or possible runtime changes. For instance, even if on-*siteTreatment* finishes punctually without delays, the following missions still wait for the preset 20 unit delay (as seen in Fig.5. Design Time). This delay essentially pushes their start to the 160-unit mark, potentially affecting their completion within the anticipated 300-unit timeframe.

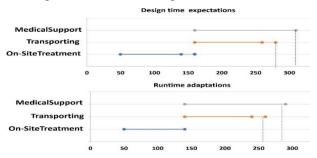


Fig. 5. Time laps during Design/Runtime of the three missions.

The gap between anticipated and realized outcomes shows a design flaw. By implementing controlled mechanisms and adaptive actions, the FESoS allows for addressing issues identified during the design phase. These corrections ensure that the three missions can be successfully accomplished within the specified time frame 300 units, Fig.5 runtime.

Fig. 6. Runtime execution and control.

The initial state of FESoS depicts three key missions connected to their associated CSs (SAMU and CivilSecurity) and requisite resources (Ambulance, MedicalEquipments, and *MedicalPersonnel*). This state also integrates FESoSResPool, representing FESoS's current resources. While the initial design may have accounted for potential delays in the on-siteTreatment mission, it didn't cater to the scenario where this mission could conclude faster than expected. This oversight causes the subsequent missions to stick to a pre-established delay. In the runtime phase (Fig. 6), if on-siteTreatment completes without delays, its delay is recalibrated from 10 units to zero. This nimble adjustment the system's responsiveness to circumstances. Consequently, the *on-siteTreatment* concludes by 140, the transporting mission wraps up at 260, and medicalSupport ends at 290. Simultaneously, the resource pool's capacity swells to 430 units, with resource allocation being 10 units for on-siteTreatment, 30 for transporting, and 60 for *medicalSupport*. This guarantees adequate resource provision for each mission. Excess resources, 10 units from transporting and 30 from medicalSupport, flow back to the resource pool, bolstering its capacity to 460 units. The successful execution of this piece of code demonstrates how

the control enables a centralized control, ensuring that the missions are done within the specified time.

C. Formal Verification

Thanks to tsearch command, we define additional RT-Maude modules to check some local/global proprieties. Due to the limited pages we are interested in checking these proprieties: (1)isDeadlineViolated: in the FESoS, timing planning ensures missions synchronize with operational schedules and resource requirements. Precise deadlines, combining expected mission duration and WCET, guarantee mission punctuality within the scenario. (2) mutual Exclusion: resource constraints enforce exclusive resource use, preventing concurrent resource sharing between missions. e.g. it ensures that different CSs' Transporting missions don't access the same ambulance simultaneously. While missions can contribute resources, they only access them when not in use elsewhere. and(3) overallMissionDuration: the entire SoS aspires to achieve its global mission within a specified timeframe. This global mission duration ensures efficient SoS operation, meeting objectives promptly. The properties reflecting SoS designers' are formalized using invariants within. For example, the timed tsearch command indicates that no state where is Deadline Violated (transporting) falls within the time frame of 240 to 260 (Fig.7) this results in a No solution outcome. This means the "isDeadlineViolated" property isn't met, and thanks to control mechanisms, any runtime delays are managed and missions are executed before their deadlines, aligning with the initial design phase.

```
(tsearch[1]{isDeadlineViolated(transporting)}=>*{isDeadlin
eViolated(transporting)} in time-interval between >= 240 and
< 260 .)
                        {mutualExclusion
(tsearch
              111
                                                (transportingSAMU.
transportingCS,
                     ambulance) }
                                     =>*
                                             {mutualExclusion
transportingSAMU, transportingCS, ambulance)} in
interval between >= 240 and < 260 .)
    rewrites: 8751 in 6374638180ms cpu (139ms real) (0 rewrites/second)
    Timed search [1] in TEST-MANY-RTTS
       {isDeadlineViolated(transporting)} =>* {isDeadlineViolated(
    transporting)}
in time between >= 100 and < 200 and with mode default time increase 1 :
    No solution
```

Fig. 7. Search results of Transporting mission.

V. RELATED WORK

In this section, we review relevant approaches to our paper's proposals. In [5], the authors have employed Maude rewriting logic framework to create an executable specification that incorporates quantitative data and resource constraints. This technique allows for comparisons of provisioning strategies to enhance process efficiency. While it provides a systematic way to optimize performance through quantitative analysis, it focuses primarily on provisioning strategy comparisons and may overlook other factors impacting efficiency, like organizational structure and external temporal dependencies. Additionally, it assumes BPMN models conform to an extension with quantitative data, which may not always hold in real-world scenarios. In [6], the authors showcase the practical application of RT-Maude tool in specifying and analyzing the CASH scheduling algorithm. Utilizing RT-Maude, they define, analyze, and assess different design alterations to the algorithm. Notably, this analysis uncovers intricate behaviors within the modifications that can result in missed deadlines and aims to enhance overall system performance and meet critical activity deadlines. However, it's essential to note that the resource allocation strategy of this algorithm may not be suitable for all types of RT-systems.

In the paper [7], an approach is introduced to aid SoS architects in constructing models for SoS configurations. This approach involves adapting UPDM views and employing SysML notations to define boundaries, detail activities, organize constituents, and design configurations. It offers a systematic method for architects to design SoS configurations effectively, ensuring that the models accurately represent the configuration objectives in an SoS. In a subsequent work [8], the authors expand upon this framework by introducing reconfiguration patterns and processes. They emphasize the importance of defining constraints, employing a transition architecture, and creating iterative and reconfiguration scripts. While this process provides a strong foundation, it also limits the autonomous executability and manageability of the process to specific characteristics when compared to our approach. The Dynamic-SoS approach [9] focuses on predicting and assessing the dynamic behavior of SoS architectures during the design phase, offering tools to characterize architectural changes and validate them through case studies. However, it lacks specific runtime control capabilities, missing the opportunity to employ quantitative controllers for optimizing SoS behavior during operations. On the other hand, SosADL [10] [11] presents an architectural description language based on π-Calculus with Concurrent Constraints, tailored for SoS architectures. It supports evolutionary architectures and automated verification but may benefit from further development in incorporating quantitative properties for real-world applications.

Studies [12] and [13] have introduced a core ontology for missions and capabilities in CSs, emphasizing resourcerelated aspects. This ontology covers a range of concept types, including physical objects, people, information, and their interactions, aiming to enhance the understanding of resource dynamics within SoSs. However, it lacks an executable environment and temporal information, limiting its capability to accurately model and analyze complex SoS interactions. In contrast, our previous work [2] proposed a comprehensive approach that leverages Maude to specify and model various missions in SoSs. This approach demonstrated Maude's robust tool support and expressive capabilities, showcasing how it can easily handle components like Missions, Resources, Roles, and their interactions with SoS management in a Direct SoS setting. The paper [14] has presented a formal model based on Maude Strategy language to handle dynamic reconfiguration in Smart SoS. The model enables the execution and analysis of Smart SoS. Maude strategies are utilized to specify dynamic reconfiguration, and their execution showcases the application of multiple crisis scenarios to achieve SoS missions. This work, although it focuses on modeling and managing SoSs and addresses same domains, it specifically don't consider the quantitative aspects of SoSs and their controlled mechanisms. The papers [15][16][17][19] have presented models to handle conflicts arising from resource consumption in SoSs. However, these models focused solely on resource consumption and did not address the production of resources at runtime.

VI. CONCLUSION

This paper presented a formal approach for analyzing and specifying temporal aspects and resource allocation in SoSs with a specific focus on their control. Firstly, the approach starts by leveraging the selecting Time-Resource strategies to select the best path that can reach the global goal of SoS. Secondly, it enables dynamic changes related to time bound

missions and resource allocation, enhancing system performance and control. Lastly, the use of Maude's formal analysis language and tools adds rigor to the evaluation of model specifications, ensuring their compliance with desired properties and enabling the model checking of potential issues. Overall, the proposed approach contributed to improve the mission execution and system performance in dynamic and complex environments.

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