

Polyelectrolyte Brush Interacting with Ampholytic Nanoparticles as Coarse-Grained Models of Globular Proteins: Poisson–Boltzmann Theory

Tatiana O Salamatova, Mikhail Y Laktionov, Ekaterina B Zhulina, Oleg V.

Borisov

▶ To cite this version:

Tatiana O Salamatova, Mikhail Y Laktionov, Ekaterina B Zhulina, Oleg V. Borisov. Polyelectrolyte Brush Interacting with Ampholytic Nanoparticles as Coarse-Grained Models of Globular Proteins: Poisson–Boltzmann Theory. Biomacromolecules, 2023, 24 (6), pp.2433-2446. 10.1021/acs.biomac.2c01153 . hal-04306914

HAL Id: hal-04306914 https://univ-pau.hal.science/hal-04306914v1

Submitted on 25 Nov 2023

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



pubs.acs.org/Biomac

Article

Polyelectrolyte Brush Interacting with Ampholytic Nanoparticles as Coarse-Grained Models of Globular Proteins: Poisson–Boltzmann Theory

⁴ Tatiana O. Salamatova, Mikhail Y. Laktionov, Ekaterina B. Zhulina, and Oleg V. Borisov*



18 electrostatic free energy of the particle is negative inside the brush and absorption is thermodynamically favorable. In the latter case, 19 the insertion free energy exhibits a local maximum (potential barrier) at the entrance to the brush. An increase in pH leads to the 20 shallowing of the free energy minimum inside the brush and a concomitant increase in the free energy maximum, which may result in 21 kinetic hindering of NP uptake. Upon further increase in pH the insertion free energy becomes positive, making NP absorption 22 thermodynamically unfavorable. An increase in salt concentration diminishes the depth of the free energy minimum inside the brush 23 and eventually leads to its disappearance. Hence, in accordance with existing experimental data our theory predicts that an increase 24 in salt concentration suppresses absorption of NPs (protein globules) by PE brush in the vicinity of IEP. The interplay between 25 electrostatic driving force for NP absorption and osmotic repelling force (proportional to NP volume) indicates that for large NPs 26 with relatively small number of ionizable groups osmotic repulsion overcomes electrostatic attraction preventing thereby absorption 27 of NPs by PE brush.

1. INTRODUCTION

²⁸ Electrostatic interactions between charged biomacromolecules ²⁹ and proteins play an important role in many biological ³⁰ processes.¹⁻⁴ A better understanding of the interactions ³¹ between natural polyelectrolytes and proteins could thus ³² have both fundamental scientific importance and direct ³³ medical implications. Synthetic polyelectrolytes (PEs) and ³⁴ colloidal polyelectrolyte nanostructures could mimic natural ³⁵ polyelectrolytes and their assemblies to unravel mechanisms of ³⁶ molecular processes in living nature, including those of direct ³⁷ medical relevance (e.g., inflammation or coagulation cascades). ³⁸ On the other hand, colloidal PE nanostructures, such as ³⁹ polyelectrolyte brushes, microgels, or block polyelectrolyte ⁴⁰ micelles can be used in medical and biotechnological ⁴¹ applications (e.g., drug and gene delivery, inhibition of viral ⁴² infection, etc.).⁵⁻¹⁴

16 NP distance from the grafting surface. It is demonstrated that, at a 17 pH value below or slightly above the isoelectric point (IEP), the

⁴³ PE brushes (layers of charged macromolecules terminally ⁴⁴ attached to a planar substrate or to the surface of colloidal ⁴⁵ particles and immersed in aqueous solution) play a prominent role here, and their interactions with charged species have been 46 actively explored experimentally and theoretically (see ref 1 for 47 a comprehensive review). Planar, spherical, and cylindrical PE 48 brushes are distinguished according to the geometry of the 49 grafting surface. The latter closely mimic natural glycosami- 50 noglycans (GAGs) (e.g., aggrecan in articular cartilage, 51 envisioned as a cylindrical brush with keratan sulfate and 52 chondroitin sulfate side chains end-tethered to the core 53 protein¹⁵), or heparan-sulfate proteoglycans (HSPG) emanat-54 ing from the cell surface.¹⁶

pH_b=pH_{IFP}+0.5

In living systems, globular proteins interact with charged 56 biomacromolecular assemblies that often have complex brush- 57

Received: September 22, 2022 Revised: March 21, 2023

pH_b=pH_{IEP}+1.0



pH_b=pH_{IEP}

s8 like architectures (e.g., layers of bacterial extracellular s9 polysaccharides, endothelial glycocalyx, complexes of aggre-60 canes with hyaluronic acid, etc.) comprising both weak 61 (carboxyl) and strong (sulfate) anionic groups. Synthetic PE 62 brushes can be formed by macromolecules comprising either 63 strong (permanently charged) or weak (pH-sensitive) 64 ionizable groups. Proteins, on the other hand, are weak 65 polyampholytes (PAs) that bear pH-sensitive cationic and 66 anionic groups on their surface. Hence, the net charge of the 67 protein globule depends on pH, and vanishes in the so-called 68 isoelectric point, pH_{IEP}, in which the net charges of cationic 69 and anionic groups exactly match each other. Hence, the 70 protein globule possesses a net positive or negative charge at 71 pH \leq pH_{IEP} or pH \geq pH_{IEP}, respectively.

⁷² Under physiological conditions, biomacromolecular brushes ⁷³ and most of globular proteins are similarly (negatively) ⁷⁴ charged, so that their interactions could be mediated by the ⁷⁵ Coulomb electrostatic repulsions. On the other hand, seminal ⁷⁶ works of M. Ballauff and co-workers convincingly demon-⁷⁷ strated that synthetic polyanionic brushes can efficiently uptake ⁷⁸ globular proteins above (on the "wrong side") the IEP, that is, ⁷⁹ when the PE brush and the protein are both negatively ⁸⁰ charged.^{17–20} It was also demonstrated that absorption of the ⁸¹ proteins is efficient at low and suppressed at high ionic ⁸² strength due to the electrostatic nature of attraction between ⁸³ similarly (negatively) charged PE brushes and proteins.

Two possible mechanisms were proposed to explain this 84 85 experimental observation: First, it was suggested that, due to the Donnan equilibrium, pH inside the polyanionic brush may 86 87 be lower than pH_{IEP} even when pH in the buffer is higher than pH_{IEP} so that the protein which is negatively charged in the 88 89 buffer, acquires positive charge inside the negatively charged 90 brush and, therefore, is spontaneously absorbed by the 91 brush.²¹⁻²³ An alternative hypothesis exploits the fact that 92 cationic and anionic groups on the protein globule surface are 93 distributed inhomogeneously and give rise to "patches" of 94 positive and negative charges. Even when in total the globule is 95 charged negatively, adsorption of the brush-forming polyanions 96 on the (minority) patches of positive charge leads to the gain 97 in the electrostatic free energy which overcompensates the free 98 energy losses due to depletion from the negatively charged 99 patches.^{24,25} Recent experiments on complexation between 100 polyelectrolytes and green fluorescent protein mutants with 101 varied patchiness in the surface charge distribution²⁶ 102 convincingly supports the importance of this mechanism of 103 polyelectrolyte-protein binding. Both hypotheses provide 104 qualitatively plausible explanation of the protein absorption 105 by similarly charged PE brushes though both lack quantitative 106 theoretical justification. Presumably, the reionization may 107 serves as the dominant driving force for binding of proteins 108 with fairly uniform (nonpatchy) distribution of cationic and 109 anionic groups on the globule surface, by strongly charged PE 110 brushes, including biological ones (e.g., HSPG). This is in a 111 line with results of numerical self-consistent field calculations 112 for protein-like ampholytic particles interacting with planar PE 113 brushes²³ and molecular dynamics simulations of short 114 ampholytic molecules interacting with a starlike PE.²⁷ At the 115 same time, the short-range nonelectrostatic interactions 116 between protein amino acid residues and the brush monomer 117 units could also be significant, and in a general case, absorption 118 of proteins by PE brushes is governed by both types of 119 interactions.²⁰

In our recent paper²⁸ we have demonstrated that charge 120 inversion due to reionization of a weak ampholytic nano- 121 particle (NP) upon insertion into a similarly charged PE brush 122 or microgel is a necessary but insufficient condition for the 123 negative balance in the differential free energy. In other words, 124 even if the NP, being negatively charged in the buffer, acquires 125 a positive charge inside the negatively charged brush, the net 126 ionic interaction balance may disfavor its uptake by the brush. 127 This qualitative conclusion was made on the basis of a simple 128 Donnan model that disregards the spatial distribution of an 129 electrostatic field inside the PE brush/microgel. 130

Advances in the theory of polyelectrolyte brushes^{29,30,32} 131 provide a full quantitative analytical description of the 132 electrostatic potential and local concentrations of mobile 133 ions inside and outside of planar PE brushes within the 134 accuracy of the Poisson–Boltzmann approximation. This 135 theoretical approach has been recently extended³³ to brushes 136 formed by branched polyelectrolytes that mimic natural 137 biomacromolecular brushes, and can be applied with 138 reasonable accuracy to PE brushes on surfaces of large 139 colloidal particles.³⁴

In this study, we focus exclusively on the electrostatic driving 141 forces with aim to unravel different mechanisms regulating 142 uptake of nanoparticles and globular proteins by PE brushes. 143 We assimilate globular proteins to weak polyampholytic 144 nanoparticles (NPs) with fixed volume and surface area 145 covered with both acidic and basic ionizable groups. Although 146 such coarse-graining of globular proteins is rather reduction- 147 istic, it could still illuminate general trends in the electrostatic 148 regulation of the protein-PE brush interactions. The aim of the 149 present paper is to implement the Poisson-Boltzmann 150 framework to analyze the position-dependent ionization and 151 insertion free energy of weak (pH-sensitive) polyampholytic 152 NPs, and to examine the effect of environmental conditions 153 (pH, salt concentration) and the brush grafting density on the 154 shape of insertion free energy curves. This approach provides 155 the distribution profiles of NPs inside the brush and may be 156 further used to access the diffusion rates of NPs through PE 157 brushes. 158

The rest of the paper is organized as follows: In section 2 we 159 introduce our theoretical model and present dominant 160 contributions to the NP free energy in the brush. A brief 161 summary on the Poisson—Boltzmann theory of PE brushes and 162 the review of electrostatic potential distribution is given in 163 section 3, while more detailed derivations are delegated to the 164 SI. Sections 3.1 and 3.2 are devoted to formulation of the 165 electrostatic and osmotic contributions to the insertion free 166 energy, respectively. The insertion free energy profiles 167 calculated under varied conditions for NPs with one anionic 168 and one cationic type of ionizable sites are presented in section 169 3.3. Finally, in section 4 we overview the results and outline 170 our conclusions. 171

2. METHOD

2.1. Model. We consider a polyampholytic nanoparticle 172 (NP), as a model of a protein in its globular conformation, that 173 comprises N_+ ionogenic groups (sites) capable of acquiring 174 positive (elementary) charge upon protonation, and N_- 175 monomer units capable of acquiring negative (elementary) 176 charge upon dissociation of hydrogen ion. The NP has volume 177 *V* and ionizable groups are assumed to be evenly distributed on 178 its surface with area Σ .

In the general case, the NP might contain several types of 181 cationic and anionic ionogenic groups (i.e., amino acid 182 residues), each characterized by specific acidic ionization 183 constant $K_{i\pm}$. We ascribe the ionization constant K_{i-} to N_{i-} 184 anionic groups ($i_{-} = 1, 2, ...$) and the ionization constant K_{i+} to 185 N_{i+} cationic groups ($i_{+} = 1, 2, ...$). Hence, the total number of 186 ionizable groups is

$$N_{\Sigma} = N_{+} + N_{-} = \sum_{i+} N_{i+} + \sum_{i-} N_{i-}$$
(1)

f1

187

The NP is interacting with a polyelectrolyte brush, Figure 1. 189 The brush is formed by strong (quenched) polyelectrolytes

Figure 1. Schematics of an ampholytic NP insertion into a polyelectrolyte brush. Blue, red, and white areas on the globule surface correspond to cationic, anionic, and neutral residues, respectively.

190 (polyacids) with degree of polymerization $N \gg 1$ end-191 tethered to the surface with density $\sigma = a^2/s$ (*a* is length of 192 monomer unit and *s* is the grafting area per chain). The PE 193 chains are assumed to be intrinsically flexible (with Kuhn 194 segment length on the order of monomer unit length, *a*), and 195 have a fraction α of (negatively) charged monomer units.

The pH in the solution (in the buffer) is fixed to the value of pH_b . The solution contains monovalent (positively and negatively charged) mobile ions of low molecular weight salt solution (number density)

$$c_{b+} = c_{b-} = c_s$$
 (2)

that controls the Debye screening length

$$c^{-1} = (8\pi l_{\rm B} c_{\rm s})^{-1/2} \tag{3}_{202}$$

Here, $l_{\rm B} = e^2/ck_{\rm B}T$ is the Bjerrum length (*e* is the elementary 203 charge, *e* is the dielectric permittivity of the solvent, $k_{\rm B}$ is the 204 Boltzmann constant, and *T* is the temperature). In the 205 following we assume that $l_{\rm B} = a$, which leads to the 206 proportionality factor \approx 5 between molar concentration and 207 volume fraction $C_{\rm s} = c_{\rm s}a^3$ of the salt ions.

Because of excess electrostatic potential $\Psi(z) \leq 0$ created by 209 PE brush at distance z from the grafting surface (with the 210 reference value $\Psi(z = \infty) = 0$), and respective gradient in the 211 local concentration of hydrogen ions, the replacement of the 212 NP from buffer solution into PE brush at distance z is 213 accompanied by reionization of its cationic and anionic groups, 214 and leads to the concomitant change in the NP free energy, 215

$$\Delta F(z) = \Delta F_{\rm ion}(z) + \Delta F_{\rm vol}(z) \tag{4}$$

Here, $\Delta F_{\text{ion}}(z)$ and $\Delta F_{\text{vol}}(z)$ account for reionization free 217 energy and for the work against excess osmotic pressure inside 218 the brush, respectively. 219

2.2. Electrostatic Potential of a Quenched Polyelec- ²²⁰ **trolyte Brush.** The reduced self-consistent electrostatic ²²¹ potential, $\psi(z) \equiv e\Psi(z)/k_{\rm B}T$, in a negatively charged (anionic) ²²² PE brush can be presented as ²²³

$$\psi_{\rm in}(z) = \frac{z^2 - H^2}{H_0^2} + \psi_{\rm in}(H), \ 0 \le z \le H$$
(5) 224

Here, z is the distance from the grafting surface, H is the total 225 thickness of the brush (cutoff of the polymer density profile), 226 and H_0 is the characteristic length 227

$$H_0/a = \sqrt{\frac{8}{3\pi^2}} N \alpha^{1/2}$$
 (6) 228

The value of constant $\psi_{in}(H)$ depends on the potential 229 calibration, and ensures continuity of the potential at the brush 230 edge, $\psi_{in}(H) = \psi_{out}(H)$. The potential outside the brush, 231 $\psi_{out}(z)$, coincides with that of a uniformly charged plane with 232 the surface charge per unit area equal to the residual (negative) 233 charge per unit area of the brush 234

$$\tilde{q} = \int_{0}^{H} \rho(z) dz = -\frac{H}{2\pi l_{\rm B} H_0^2}$$
(7) ₂₃₅

with the residual charge density ho(z) specified by the Poisson 236 equation, 237

$$\frac{d^2 \psi_{\rm in}(z)}{dz^2} = -4\pi l_{\rm B} \rho(z) \tag{8}_{238}$$

(Here and below, charge is measured in the elementary charge, 239 e, units.) The electrostatic potential outside the brush is thus $240 formulated as^{30}$ 241

$$\psi_{\rm out}(z) = -2 \ln \left[\frac{(\kappa \tilde{\Lambda} + \sqrt{(\kappa \tilde{\Lambda})^2 + 1} - 1) + (\kappa \tilde{\Lambda} - \sqrt{(\kappa \tilde{\Lambda})^2 + 1} + 1)e^{-\kappa(z-H)}}{(\kappa \tilde{\Lambda} + \sqrt{(\kappa \tilde{\Lambda})^2 + 1} - 1) - (\kappa \tilde{\Lambda} - \sqrt{(\kappa \tilde{\Lambda})^2 + 1} + 1)e^{-\kappa(z-H)}} \right]$$
(9)

С

.

242 243

244

with the Gouy-Chapman length



201

246

254

$$\tilde{\Lambda} = \frac{1}{2\pi l_{\rm B} |\tilde{q}|} = \frac{H_0^2}{H} \tag{10}$$

247 The latter controls distributions of the electrostatic potential 248 and small mobile ions outside the brush, i.e., at $z \ge H$. The 249 potential defined by eq 9 vanishes at $z \to \infty$. The cutoff of the 250 polymer density profile, z = H, is found from the condition of 251 conservation of number of monomer units in grafted chains. 252 The minimal value reached by the electrostatic potential at the 253 grafting surface, z = 0,

$$\psi_{\rm in}(0) = -\frac{H^2}{H_0^2} + \psi(H) = -\frac{H^2}{H_0^2} + 2\ln\left[\frac{\sqrt{(\kappa\tilde{\Lambda})^2 + 1} - 1}{\kappa\tilde{\Lambda}}\right]$$
(11)

255 is the increasing function of salt concentration c_s in the buffer 256 but the decreasing function of the grafting density σ . However, 257 the potential difference across the brush,

$$-\psi_{\rm in}(0) + \psi(H) = \frac{H^2}{H_0^2}$$
(12)

259 decreases as a function of salt concentration and increases 260 upon an increase in the grafting density, because the brush 261 thickness H decreases as a function of salt concentration, but 262 increases as a function of σ .

263 The polymerization degree N of the grafted PE chains 264 weakly affects $\psi(0)$, while the brush thickness $H \sim N$. More 265 detailed derivation and typical shapes of the electrostatic 266 potential profile inside and outside the brush are presented in 267 SI.

Notably, the parabolic shape of electrostatic potential $\psi_{in}(z)$ 269 in eq 5 holds if the stretched brush-forming chains are still far 270 from full extension (i.e., $H \le L = aN$). An approach to full 271 extension of the tethered PE chains $(H \rightarrow L)$ modifies 272 electrostatic potential $\psi_{in}(z)$ as³¹

$$\psi_{\rm in}(z) = \frac{3}{\alpha} \ln \frac{\cos(\pi z/2L)}{\cos(\pi H/2L)}$$

273 Electrostatic potential $\psi_{out}(z)$ outside strongly stretched PE 274 brush is given by eq 9 with renormalized Gouy–Chapman 275 length

$$\tilde{\Lambda} = \frac{H_0^2}{H} \frac{(\pi H/2L)}{\tan(\pi H/2L)}$$

276 In the following we assume that the tethered PEs are 277 moderately charged (with degree of ionization $\alpha < 1$) to 278 ensure the parabolic shape of $\psi_{in}(z)$.

3. RESULTS AND DISCUSSION

284

3.1. Ionic Contribution to the Free Energy. Transfer of 280 NP from the bulk of solution in PE brush is accompanied by 281 the change in ionization states of both basic and acidic groups 282 on NP surface. The ionic part of the differential free energy can 283 be expressed as²⁸

$$\Delta F_{\rm ion}(z)/k_{\rm B}T = \sum_{i+} N_{i+} \ln\left(\frac{1-\alpha_{i+}(z)}{1-\alpha_{bi+}}\right) + \sum_{i-} N_{i-} \ln\left(\frac{1-\alpha_{i-}(z)}{1-\alpha_{bi-}}\right)$$
(13)

285 where α_{bi+} , $\alpha_{i+}(z)$, α_{bi-} , and $\alpha_{i-}(z)$ are the respective degrees of 286 ionization of basic and acidic monomer units on the surface of 287 NP placed at distance z from the grafting surface and in the 288 bulk of the solution (at $z = \infty$). 289 Here,

$$\begin{aligned} \alpha_{i+}(z) &= (1 + K_{i+}/[H^+(z)])^{-1} \equiv (1 + 10^{\text{pH}(z) - \text{pK}_{i+}})^{-1} \\ &= \left(1 + \frac{1 - \alpha_{bi+}}{\alpha_{bi+}} \exp(\psi(z))\right)^{-1} \end{aligned}$$
(14) 290

and

$$\begin{aligned} \alpha_{i-}(z) &= (1 + [H^{+}(z)]/K_{i-})^{-1} \\ &\equiv (1 + 10^{pK_{i-}-pH(z)})^{-1} \\ &= \left(1 + \frac{1 - \alpha_{bi-}}{\alpha_{bi-}} \exp(-\psi(z))\right)^{-1} \end{aligned}$$
(15) 292

The respective degrees of ionization of ionogenic groups $i\pm$ in 293 the buffer are 294

$$\alpha_{bi+} = (1 + K_{i+} / [H^+]_b)^{-1} = (1 + 10^{\text{pH}_b - \text{pK}_{i+}})^{-1}$$
(16) 295

and

$$\alpha_{bi-} = (1 + [H^+]_b / K_{i-})^{-1} = (1 + 10^{pK_{i-} - pH_b})^{-1}$$
(17) ₂₉₇

 $[H^+(z)]$ is the local concentration of hydrogen ions (specifying 298 local pH(z) = $-\log[H^+(z)]$), pH_b \equiv pH(z = ∞) = 299 $-\log[H^+(z = \infty)]$, and K_{i+} and K_{i-} are respective acidic 300 ionization constants of basic and acidic groups. 301

According to eqs 14 and 15, ionization of acidic and basic 302 ionogenic groups is controlled by local electrostatic potential 303 $\psi(z)$ in the brush, while the Coulomb interactions between 304 ionized groups on NP surface are disregarded. These 305 interactions could shift the ionization constants with respect 306 to "bare" constants K_{i+} and K_{i-} (see refs 35 and 36). Within 307 the applied here approximation, $\{N_{i\pm}\}$ and $\{K_{i\pm}\}$ are 308 considered as independent sets of variables. We also neglect 309 the electrostatic potential gradient on the length scale of NP 310 spatial dimensions. 311

The spacial distribution of hydrogen ions can be expressed 312 as 313

$$[H^{+}(z)] = [H^{+}]_{b} \exp(-\psi(z))$$
(18) 314

As long as hydrogen ions are distributed between PE brush 315 and solution according to eq 18, lower electrostatic potential 316 inside the brush, $\Psi(z) \leq 0$, indicates that local concentration 317 of H^+ ions inside the brush is larger than in the bulk of the 318 solution. As a result, the degree of ionization of basic residues 319 inside polyanionic brush is higher, while the degree of 320 ionization of acidic residues is lower than in the bulk of the 321 solution (eqs 14 and 15). The sign of $\Delta F_{ion}(z)$ is determined 322 by the balance between reionization free energies of basic and 323 acidic monomer units (the first and the second terms in eq 13, 324 respectively). 325

The net charge on NP (measured in the elementary charge 326 units *e*) depends on its position *z* with respect to the grafting 327 surface and can be expressed as 328

$$Q(z) = \sum_{i+} N_{i+} \alpha_{i+}(z) - \sum_{i-} N_{i-} \alpha_{i-}(z)$$
(19) ₃₂₉

while the NP charge in the buffer is given by

$$Q_{b} = Q(z = \infty) = \sum_{i+} N_{i+}\alpha_{bi+} - \sum_{i-} N_{i-}\alpha_{bi-}$$
(20) 331

The isoelectric point, pH_{IEP} , corresponds to pH_b at which the 332 NP charge in the buffer vanishes, $Q_b = 0$. 333

We focus primarily on the case of $pH_{b} \ge pH_{IEP}$, that is, when 334 the NP in the bulk of the solution is charged negatively, 335

330

291

296

336 $Q_b \leq 0$, i.e., similarly to the brush. Because the electrostatic 337 potential $\psi(z)$ created by the brush is a monotonically 338 increasing function of z (i.e., monotonically increasing in 339 absolute value upon approaching the grafting surface), the net 340 charge of the NP Q(z) monotonically increases upon 341 approaching the grafting surface and, depending on the sets 342 of parameters $\{N_{i\pm}, K_{i\pm}\}, \{c_s, pH_b\}, \{\alpha, N, \sigma\}$, may remain 343 negative or invert its sign to positive at some particular 344 distance z^* from the grafting surface, so that

$$Q(z=z^*)=0$$

345 Remarkably, z^* may correspond to the NP position either 346 inside, or outside the brush (close to its edge). The position z^* 347 can be found from the equation

$$\psi(z^*) = -\Delta p H_b / \log_{10} e \approx -2.3 \Delta p H_b$$
⁽²¹⁾

349 with

Δ

3

353

359

$$\Delta pH_{h} = pH_{h} - pH_{IFP}$$

350 which implies (with the account of eq 18) that local 351 pH($z = z^*$) at $z = z^*$ coincides with pH_{IEP} for NP in solution. 352 Using eqs 13 and 19, one can demonstrate that

$$\int_{B} \left(\frac{\partial \Delta F_{\rm ion}(z)}{\partial z} \right)_{z^*} = 0$$
(22)

354 that is, the ionization free energy passes through a maximum at 355 $z = z^*$, i.e., in the point of the charge inversion. Indeed,

$$\frac{\partial \Delta F_{\rm ion}(z)}{\partial z} = \frac{\partial \Delta F_{\rm ion}}{\partial \lambda} \cdot \frac{\partial \lambda(z)}{\partial z}$$

356 where $\lambda(z) \equiv \exp(\psi(z))$. By taking the derivative of the r.h.s. 357 of eq 13 with respect to $\lambda(z)$ (with the account of eqs 14 and 358 15), one arrives at

$$\frac{\partial \Delta F_{\rm ion}(z)}{\partial z} = \frac{1}{\lambda} \frac{\partial \lambda(z)}{\partial z} \cdot Q(z) = \frac{\partial \psi(z)}{\partial z} \cdot Q(z)$$
(23)

360 where the position-dependent charge Q(z) of NP is given by 361 eq 19. As soon as $\lambda(z)$ is a positive, monotonously increasing 362 function of z in the whole range of $z \in [0, \infty)$, eq 23 indicates 363 that $\Delta F_{ion}(z)$ exhibits a maximum in the NP charge inversion 364 point, $z = z^*$.

When $\Delta F_{\text{ion}}(z=0) \leq 0$ and $z^* \geq 0$, absorption of NP by the 366 brush is thermodynamically favorable, and the minimum in 367 $\Delta F_{\text{ion}}(z)$ (reached at the grafting surface, z=0) is separated 368 from the exterior solution by the potential barrier with the 369 height $\Delta F_{\text{ion}}(z^*)$ located at $z=z^*$. As we demonstrate below, 370 the charge inversion may occur at $z=z^* \geq 0$ even when 371 $\Delta F_{\text{ion}}(z=0) \geq 0$. In this case, the localization of positively 372 charged NP inside polyanionic brush corresponds to a 373 metastable state. Finally, when z^* decreases down to zero, 374 the charge inversion inside the brush does not take place and 375 the insertion free energy $\Delta F_{\text{ion}}(z)$ becomes a monotonically 376 decreasing function of z. As a result, the Coulomb force pushes 377 NP out of the brush and no absorption of NPs by PE brush 378 occurs spontaneously.

379 Obviously, if NP is charged positively in the solution, 380 $Q_b \ge 0$, then $\Delta F_{ion}(z) \le 0$ at $\forall z \in [0,\infty)$ and is a 381 monotonically increasing function, 382 $\partial \Delta F_{ion}(z)/\partial z \ge 0 \ \forall z \in [0,\infty)$.

383 3.2. Osmotic Contribution to the Free Energy. The **384** second term in eq 4 accounts for the work against excess

392

osmotic pressure of mobile ions inside the brush and in the 385 double electrical layer outside. If the concentrations of mobile 386 monovalent ions of low molecular weight salt in the buffer (at 387 $z = \infty$) are $c_{b+} = c_{b-} = c_{s}$, then their concentrations at arbitrary 388 distance *z* from the grafting surface are given by the Boltzmann 389 law, 390

$$c_{\pm}(z) = c_{\rm s} \, \exp(\mp \psi(z))$$
 (24) 391

and the excess osmotic pressure is

$$\Pi(z)/k_{\rm B}T = c_{+}(z) + c_{-}(z) - 2c_{\rm s} =$$
(25) 393

$$c_{\rm s}(\exp(\psi(z)/2) - \exp(-\psi(z)/2))^2 = 4c_{\rm s} \sinh^2(\psi(z)/2)$$
(26) 394

Hence, the osmotic contribution to the insertion free energy, 395

$$\Delta F_{\rm vol}(z)/k_{\rm B}T = 4Vc_{\rm s} \sinh^2(\psi(z)/2)$$
(27) (27) (27)

is proportional to NP volume V and monotonically decreases 397 with z. Hence, the derivative of this second term in the free 398 energy in eq 4 always provides a thermodynamic force 399 expelling the NP from the brush. 400

We remark that in sufficiently dense or/and weakly charged 401 brushes the nonelectrostatic (excluded volume) interactions 402 provide the dominant contribution to the osmotic pres- 403 sure.^{37–39} However, in the present work we focus at sufficiently 404 strongly charged brushes in which the electrostatic interactions 405 dominate over the short-range repulsions between monomer 406 units. 407

3.3. NP with Two Types of lonizable Sites. Below we 408 focus on a particular case when the NP comprises one type of 409 cationic groups with ionization constant K_+ and one type of 410 anionic groups with the ionization constant K_- . This 411 simplification allows us to analyze the main trends in NP 412 interaction with PE brush at variable environmental conditions 413 (pH_b and c_s) and NP volume V. 414

The fraction of positively charged ionizable monomer units 415 is defined as 416

$$f_{+} = \frac{N_{+}}{N_{-} + N_{+}} \equiv \frac{N_{+}}{N_{\Sigma}}$$
(28) 417

where $N_{+} + N_{-} = N_{\Sigma}$ is the total number of ionizable (basic 418 and acidic) groups, and the ionic contribution ΔF_{ion} in eq 13 419 with $i_{+} = i_{-} = 1$ reduces to 420

$$\Delta F_{\rm ion}(z)/k_{\rm B}T = N_{\Sigma} \left[f_{+} \ln \left(\frac{1 - \alpha_{+}(z)}{1 - \alpha_{b+}} \right) + (1 - f_{+}) \ln \left(\frac{1 - \alpha_{-}(z)}{1 - \alpha_{b-}} \right) \right]$$
(29) 421

In section 3.3.1, we start with the analysis of $\Delta F_{\rm ion}(z)$, which 422 is the dominant contribution to the overall free energy, 423 $\Delta F(z) \approx \Delta F_{\rm ion}(z)$, in the case of small NPs. In the following 424 section 3.3.2 we consider the interplay between $\Delta F_{\rm ion}(z)$ and 425 $\Delta F_{\rm vol}(z)$ which becomes essential for increasingly bulky 426 charged species and may prevent NP absorption by PE 427 brush even if the reionization free energy, $\Delta F_{\rm ion}$, provides a 428 driving force for it.

3.3.1. Reionization Free Energy for NP Interacting with 430 Polyelectrolyte Brush. Below we present typical ionization free 431 energy profiles $\Delta F_{ion}(z)$ normalized by the total number of 432 ionizable sites N_{Σ} calculated for the NP with $f_+ = 0.5$ at varied 433 pH_b, reduced salt concentration $C_s = c_s a^3$ and grafting density 434 $\sigma = a^2/s$. We use model equal values of ionization constants 435 pK_ = pK_+ = 5 that assures maximal impact of the reionization 436 f2

f3

437 free energy to the overall insertion free energy balance and 438 corresponds at $f_+ = 0.5$ to the IEP pH_{IEP} = 5. In real experiment 439 chosen parameters are sufficiently close to the p K_- value for 440 carboxylic groups and not far from p K_+ value for, e.g., 441 N(CH₃)₂ groups.

⁴⁴² The degree of polymerization of the brush-forming chains ⁴⁴³ N = 300. Notably, C_s and σ affect the magnitude of the excess ⁴⁴⁴ electrostatic potential created by the brush, whereas pH_b ⁴⁴⁵ controls degrees of ionization of the cationic and anionic ⁴⁴⁶ residues and the net charge of the globule Q_b in the buffer.

447 In Figure 2a,b, the position-dependent free energy $\Delta F_{ion}(z)$ 448 and charge Q(z) are plotted as a function of distance z from



Figure 2. Position-dependent insertion free energy $\Delta F_{ion}(z)$ (a) and the NP charge Q(z) (b) both normalized by $N_{\Sigma t}$ as a function of the distance z from the grafting surface for a series of pH_b values around the IEP at fixed salt concentration $C_s = 10^{-3}$. Arrows indicate the upper boundary of the brush. Dashed vertical lines indicate the charge inversion point, $z = z^*$. Dashdot horizontal lines indicate $\Delta F_{ion}(z) = 0$ and Q(z) = 0. Colored circles in panels (a) and (b) correspond to the charge inversion points $z = z^*$.

⁴⁴⁹ the grafting surface for a series of pH_b values at constant salt ⁴⁵⁰ concentration $C_s = 10^{-3}$.

In Figure 3a,b, we show cross sections of 2D profiles of the sinsertion free energy $\Delta F_{ion}(z, \Delta pH_b)$, and net charge $A_{53} Q(z, \Delta pH_b)$ of the NP plotted at three selected values of salt concentration C_s

As one can see from Figures 2b and 3b and follows from eq 456 19, because of reionization of cationic and anionic sites in the 457 electrostatic potential of the polyanionic brush, net charge 458 Q(z) of the NP is always a decreasing function of z.

Sufficiently far above the IEP (e.g., at $\Delta pH_b = 1.3$ in Figure 460 2a,b), the NP is negatively charged in the buffer and remains 461 negatively charged, $Q(z) \leq 0 \quad \forall z \in [0,\infty)$, though |Q(z)|462 decreases in the absolute value upon insertion of the NP into 463 the brush. The insertion free energy in this case is positive, 464 $\Delta F_{ion}(z) > 0 \quad \forall z \in [0,\infty)$, and monotonously decreasing



Figure 3. Cross sections of the 2D profiles of the insertion free energy $\Delta F_{ion}(z, \Delta pH_b)$ (a) and NP charge $Q(z, \Delta pH_b)$ (b), both normalized by N_{Σ} , for a set of values of salt concentration (with the corresponding color code, as indicated at the curves). Colored circles in panel (a) indicate points of vanishing free energy, $\Delta F_{ion}(z, \Delta pH_b) = 0$; colored circles in panel (b) correspond to the charge inversion points $z = z^*$.

function of z, $\partial \Delta F_{ion}(z)/\partial z \leq 0$, that is, the NP is expelled 465 from the brush.

On the contrary, below the IEP, at $\Delta pH_b < 0$, the charge of 467 the NP is positive, $Q(z) > 0 \ \forall z \in [0,\infty)$ (Figures 2b and 3b). 468 The free energy $\Delta F_{ion}(z) < 0 \ \forall z \in [0, \infty)$ is negative and 469 monotonously decreases upon approaching the grafting surface 470 (Figures 2a and 3a). In this case, the NP and the brush are 471 oppositely charged, and the NP is driven into the brush by the 472 attractive Coulomb force. The depth of the free energy edge 473 minimum at the grafting surface, $\Delta F_{ion}(z = 0)$, grows upon a 474

> https://doi.org/10.1021/acs.biomac.2c01153 Biomacromolecules XXXX, XXX, XXX–XXX

495

475 decrease in ΔpH_b , or upon an increase in the magnitude of the 476 negative electrostatic potential at the surface which can be 477 induced either by a decrease in salt concentration C_s (Figure 478 S2a) or by an increase in grafting density σ (Figure S2b). The 479 same applies also at the IEP, pH = pH_{IEP}, when the NP charge 480 is vanishing far away from the brush, but becomes positive and 481 monotonously increases when NP approaches and enters the 482 brush.

483 The most peculiar patterns in $\Delta F_{ion}(z)$ and Q(z) are 484 observed at $\Delta pH_b \ge 0$, i.e., slightly above the IEP, as illustrated 485 by Figure 2a,b and the cross-section of the $\Delta F_{ion}(z, \Delta pH_b)$ 486 surface at $\Delta pH_b = 0.4$ in Figure 3a,b. In this case NP is charged 487 negatively in the buffer, $Q_b < 0$, but inverts the sign of its 488 charge upon embedding into the brush at $z = z^*$. That is, the 489 NP charge $Q(z \ge z^*) \le 0$ and $Q(z \le z^*) \ge 0$. As 490 demonstrated above, the free energy $\Delta F_{ion}(z)$ passes through a 491 maximum in the charge inversion point $z = z^*$, i.e., $\Delta F_{ion}(z)$ is 492 an increasing function of z at $z \in [0, z^*)$ and a decreasing 493 function of z at $z \in [z^*, \infty)$. Obviously, $z^* \to \infty$ at $pH_b \to$ 494 pH_{IEP} .

In Figure 4 we present a typical zoomed profile of the free

496 energy $\Delta F_{ion}(z)$ with maximum, corresponding to the Q(z)



Figure 4. Characteristic dependence of the $\Delta F_{ion}(z)$ with a maximum at $z = z^*$ and corresponding dependence Q(z) with charge inversion at $z = z^*$ plotted for $\Delta p H_b = 0.4$ both normalized by N_{Σ} . Salt concentration is $C_s = 10^{-3}$, grafting area per chain is $s/a^2 = 100$. Arrow indicate the upper boundary of the brush (z = H), and the charge inversion point $z = z^*$ is indicated by vertical dashed line and a red circle.

⁴⁹⁷ sign inversion point, and $\Delta F_{ion}(z = 0) < 0$. This free energy ⁴⁹⁸ profile indicates the presence of electrostatic driving force for ⁴⁹⁹ NP absorption by PE brush.

Remarkably, similar patterns in the position-dependent net 500 charge were observed in Molecular Dynamic simulations²⁷ of 501 502 ampholytic oligopeptide interacting with strongly charged starlike polyelectrolyte: in the vicinity of the IEP the 503 oligopeptide charge inversion was observed upon approaching 504 the center of the star. However, quantitative comparison of our 505 results to those presented in ref²⁷ is challenging because of 506 essentially different spatial distribution of polymer density and 507 electrostatic field in a planar PE brush and in a single PE star. 508 As seen in Figure 3a,b, an increase in salt concentration (at a 509 510 given ΔpH_h leads to the shift in the charge inversion point z^* 511 toward the grafting surface, the decrease in Q(z), and 512 narrowing of the presurface potential well which simulta-513 neously becomes more shallow.

Upon a moderate increase in pH_b above the IEP, i.e., upon a s1s decrease in the NP charge $Q_b < 0$ in the buffer, the charge

inversion point z^* is shifted toward the grafting surface, the ⁵¹⁶ magnitude of the maximum in $\Delta F_{ion}(z)|_{z=z^*}$ increases, and the ⁵¹⁷ depth of the presurface potential well, $|\Delta F_{ion}(z=0)|$, decreases. ⁵¹⁸ In this regime, absorption of NPs by the brush remains ⁵¹⁹ thermodynamically favorable, but requires overcoming of the ⁵²⁰ potential barrier with maximum at $z = z^*$. At sufficiently large ⁵²¹ number of ionizable groups on NP surface, $N_{\Sigma} \sim 10^2$, the ⁵²² barrier may increase up to $\sim 10k_{\rm B}T$ thus completely hindering ⁵²³ NP absorption by PE brush kinetically.

When $\Delta p H_b$ exceeds the threshold value $\Delta p H_b^{(abs)} \ge 0$ (that 525 is, $p H_b$ exceeds $p H_b^{(abs)} > p H_{IEP}$), the free energy $\Delta F_{ion}(z)$ 526 becomes positive at $\forall z \in [0, \infty)$. The free energy minimum at 527 z = 0 remains separated from the bulk of the solution by the 528 potential barrier located at $z = z^*$. Hence, the NP location 529 inside the brush at $0 \le z \le z^*$ corresponds to a metastable 530 state although the globule possesses positive net charge, 531 $Q(z \le z^*) \ge 0$ (see, e.g., the curves corresponding to 532 $\Delta p H_b = 0.7$ in Figure 2a,b). Indeed, the local free energy 533 minimum at z = 0 is separated from the global free energy 534 minimum $\Delta F_{ion}(z = \infty) = 0$ by a potential barrier at $z = z^*$, 535 which implies that, by definition,⁴⁰ the position of the NP in 536 the brush corresponds not to an equilibrium, but to a 537 metastable state. 538

Further increase in pH_b results in simultaneous increase in 539 the magnitude of the potential barrier at $z = z^*$ and its 540 displacement toward the grafting surface and concomitant 541 decrease in the depth and width of the potential well. 542 Eventually, $z^* \rightarrow 0$, and the free energy $\Delta F_{ion}(z)$ becomes a 543 positive and monotonously decreasing function of z, so that 544 the NP-PE brush interaction becomes purely repulsive. 545

Because the position-dependent net charge Q(z) and the 546 free energy $\Delta F_{ion}(z)$ depend on the brush local electrostatic 547 potential $\psi(z)$, both properties are strongly affected by salt 548 concentration in the buffer. The magnitude of $\psi(z)$ decreases, 549 and its range shrinks as the salt concentration in the buffer 550 increases (see Figure S2a in the Supporting Information). 551 Therefore, the equilibrium absorption threshold can be crossed 552 also by an increase in the salt concentration at constant pH_b, as 553 demonstrated by series of the cross sections of the 554 $\Delta F_{ion}(z, \Delta pH_b)$ surfaces corresponding to $\Delta pH_b = 1.0$ and 555 different values of C_s in Figure 3a,b. For given set of parameters 556 $\{f_+, K_+, K_-\}$ the defined above threshold pH^(abs)_b depends on 557 salt concentration C_{sr} as demonstrated in Figure 5. 558 f5

In Figure 6a,b, we present $\Delta F_{ion}(z)$ and $\bar{Q}(z)$ profiles for a 559 f6 number of selected salt concentrations C_s and constant 560 $\Delta pH_b = 0.3$. In Figure 7a,b, we show cross sections of 2D 561 f7 profiles of the insertion free energy $\Delta F_{ion}(z, c_s)$, and net charge 562 $Q(z, c_s)$ of the NP plotted at three selected values of ΔpH_b 563 above the IEP. The values of pH_b are chosen sufficiently close 564 to pH_{IEP} so that, at low salt concentration, $C_s = 10^{-3}$, the 565 $\Delta F_{ion}(z)$ exhibits pronounced maxima at the charge inversion 566 points and the edge minima at z = 0.

An increase in salt concentration leads to weakening of the 568 electrical field created by PE brush, and the magnitude of the 569 electrostatic potential $|\psi(z = 0)|$ decreases. Upon an increase in 570 salt concentration, the charge inversion point $z = z^*$ is shifted 571 to a smaller z, the free energy at the grafting surface, 572 $\Delta F_{\rm ion}(z = 0)$, increases, changes its sign from negative to 573 positive, and $\Delta F_{\rm ion}(z)$ acquires a monotonously decreasing 574 shape corresponding to expulsion of NPs from PE brush. The 575 larger the ΔpH_b , the smaller the salt concentration is needed to 576 suppress charge inversion and eliminate the potential well at 577 the grafting surface.



Figure 5. Dependences of salt concentration $C_s^{(\max x)}$ corresponding to inversion of sign of $\Delta F_{ion}(z = 0)$ (dashed line) and $C_s^{(\max,\omega)}$ corresponding to inversion of sign of $\Delta F_{ion}(z = 0) + \Delta F_{vol}(z = 0)$ (solid lines) for selected values of ω (see color code in the figure) on deviation ΔpH_b from the IEP.



Figure 6. Position-dependent insertion free energy $\Delta F_{ion}(z)$ (a) and the NP charge Q(z) (b), both normalized by N_{Σ} , as a function of the distance z from the grafting surface for a series of salt concentration C_s values at $\Delta pH_b = 0.3$. Arrows indicate the salt-dependent position of the upper boundary of the brush. Dashed vertical lines indicate the charge inversion points, $z = z^*$. Dashdot horizontal lines indicate $\Delta F_{ion}(z) = 0$ and Q(z) = 0. Colored circles in panels (a) and (b) correspond to the charge inversion points $z = z^*$.

Remarkably, if $\Delta pH_b > 0$ and $Q|_{z=0} < 0$ or, on the contrary, seo $\Delta pH_b < 0$ and $Q|_{z=0} > 0$, the addition of salt does not lead to sel qualitative changes in the shape of the $\Delta F_{ion}(z)$ curves: They sez are monotonously decreasing or monotonically increasing in ses the former and in the latter case, respectively, but their set magnitudes (the height of the potential barrier or the depth of ses the potential well) as well as the range of the potential se6 (proportional to the brush thickness *H*) decrease.

587 The effect of the grafting density $\sigma = a^2/s$ on the $\Delta F_{ion}(z)$ 588 curves is illustrated by Figure 8: An increase in the grafting

f8



Figure 7. Cross sections of the 2D profiles of the insertion free energy $\Delta F_{ion}(z, c_s)$ (a) and NP charge $Q(z, c_s)$ (b), both normalized by N_{Σ} , for a set of values of pH_b (with the corresponding color code, as indicated at the curves). Colored circles in panel (a) indicate points of vanishing free energy, $\Delta F_{ion}(z, \Delta pH_b) = 0$; colored circles in panel (b) correspond to the charge inversion points $z = z^*$.

density enhances electrostatic potential, causes additional stretching of the brush-forming PE chains (an increase in the brush thickness H) and might drive NP absorption into sufficiently dense PE brush.

3.3.2. Interplay between NP Charge and Volume. For an 593 ampholytic NP (protein globule) the ionic contribution to the 594 insertion free energy $\Delta F_{ion}(z)$ is complemented by the osmotic 595 term $\Delta F_{vol}(z)$. In this subsection we unravel the competitive 596 effects of the electrostatic (attractive) and osmotic (repulsive) 597 forces on NP absorption by PE brush. 598



Figure 8. Position-dependent insertion free energy $\Delta F_{ion}(z)$ (a) and the NP charge Q(z) (b) both normalized by N_{Σ} , as a function of the distance z from the grafting surface for a series of $s = a^2/\sigma$ values at $C_s = 10^{-3}$, $\Delta pH_b = 0.4$ (with the corresponding color code, as indicated at the curves). Arrows indicate the upper boundary of the brush. Dashed vertical lines indicate the charge inversion point, z = z^* . Dashdot horizontal lines indicate $\Delta F_{ion}(z) = 0$ and Q(z) = 0. Colored circles in panels (a) and (b) correspond to the charge inversion points $z = z^*$.

While the ionic part of the insertion free energy, $\Delta F_{ion}(z)$, may exhibit different patterns as a function of z, the osmotic contribution $\Delta F_{vol}(z)$ given by eq 27 is always a positive and monotonously decreasing function of z. As a result, at $\Delta pH_b > 0$ and $\Delta F_{ion}(z) > 0$ at any $z \ge 0$, the net free energy $\Delta F(z) = \Delta F_{ion}(z) + \Delta F_{vol}(z) > 0$ as well, and NP subscription by PE brush is unfavorable. Even when the ionic interactions provide a driving force for globule absorption, (i.e., $\Delta F_{ion}(z = 0) < 0$), the net insertion free energy $\Delta F(z = 0)$ may subscription by explicitly due to the osmotic term, $\Delta F_{vol}(z = 0)$, subscription overcompensating the attractive ionic contribution.

Using eqs 4, 27, and 29, the NP insertion free energy can be presented as

$$\Delta F(z) = N_{\Sigma} \left[\int_{f_{+}} \ln \left(\frac{1 - \alpha_{+}(z)}{1 - \alpha_{b_{+}}} \right) + (1 - f_{+}) \ln \left(\frac{1 - \alpha_{-}(z)}{1 - \alpha_{b_{-}}} \right) \right] + 4\omega C_{s} \sinh^{2}(\psi(z)/2) \right]$$
(30)

613 where we have introduced the following parameter

$$\omega = V/a^{3}N_{\Sigma} \tag{31}$$

615 which is equal to the average globule volume per ionizable 616 group. Because $\Delta F_{ion}(z) \sim N_{\Sigma}$ (eq 29) and $\Delta F_{vol}(z) \sim V$ (eq 617 27), the relative strength of the osmotic and ionic 618 contributions, $\Delta F_{vol}/\Delta F_{ion}$, depends on the parameter ω . 619 Remarkably, ω is an increasing function of the globule 620 dimensions (since N_{Σ} does not grow faster than the globule 621 surface area Σ).

622 In Table 1 we list approximate estimates of the parameter ω 623 for a number of globular proteins, using values of V and N_{Σ} 624 from the literature.⁴¹ Notably, the values of ω in Table 1 625 constitute lower boundaries, since all the ionizable residues 626 (not necessarily located at the globule surface) have been 627 accounted for in the corresponding protein.

Table 1. Proteins Corresponding to the ω Coefficient

ω	name of the protein
2.0	human serum albumin
3.2	Des-Phe B1 bovine insulin
3.5	phospholipase A2 (PLA2) from Naja naja venom
3.7	lpha-lactalbumin
4.9	human interleukin-6
5.3	human hemoglobin A2
6.1	human sex hormone-binding globulin
7.5	interleukin-37
8.6	bovine β -lactoglobulin
10.3	bromoperoxidase A1
15.7	human interleukin-17A
29.2	pumpkin seed globulin

For given globule volume *V*, $\Delta F_{vol}(z)$ in eq 27 (as well as 628 $|\psi(z)|$ in eqs 5 and 9) is a decreasing function of salt 629 concentration c_s in the buffer, and an increasing function of the 630 brush grafting density $\sigma = a^2/s$.

Consider first the scenario when $\Delta pH_b \geq 0$, and the 632 $\Delta F_{ion}(z)$ curve exhibits a characteristic pattern with the 633 maximum at $z = z^*$ and the minimum at the grafting surface, 634 $\Delta F_{ion}(z = 0) \leq 0$. In this case, the ionic interactions provide a 635 driving force for the globule absorption above IEP, 636 accompanied by the NP charge reversal. In Figure 9a we 637 f9 illustrate the evolution of the insertion free energy profile, 638 $\Delta F(z) = \Delta F_{ion}(z) + \Delta F_{vol}(z)$, upon an increase in the 639 parameter ω . As one can see in Figure 9a, at small values of ω 640 (NPs with relatively small volume V and large number N_{Σ} of 641 ionizable groups) the $\Delta F(z)$ curve has the same shape as 642 $\Delta F_{ion}(z)$. That is, exhibits a maximum close to the edge of the 643



Figure 9. Total free energy curves $\Delta F(z) = \Delta F_{ion}(z) + \Delta F_{vol}(z)$ normalized by N_{Σ} corresponding to different globule volume to the number of charge ratio ω at $C_s = 0.002$ (a) and at fixed $\omega = 9.45$ and varied salt concentration C_s (b). Other parameters are $s/a^2 = 100$. The brush boundary, z = H, is indicated by the arrows. Dashdot horizontal lines indicate $\Delta F(z) = 0$.

t1

612

644 brush and reaches a negative value at the grafting surface, but 645 with the curve as a whole moving upward. Importantly, 646 position of the maximum, $z = z_{max}$ is shifted toward the 647 grafting surface with respect to z^* ($z_{max} \leq z^*$), and does not 648 correspond anymore to the globule charge inversion threshold 649 (i.e., $Q(z = z_{max}) > 0$). Further increase in the globule volume 650 V (i.e., an increase in ω) results in further shift of the 651 maximum toward the grafting surface, and the increase in both, 652 $\Delta F(z_{max})$ and $\Delta F(z = 0)$. The latter becomes eventually 653 positive indicating that the osmotic repulsion overcompensates 654 the electrostatic attraction making globule absorption 655 thermodynamically unfavorable. At large ω , $\Delta F(z)$ become a 656 monotonously decreasing function of z with $\Delta F(z) > 0$ at any 657 $z \ge 0$.

An increase in salt concentration leads to the simultaneous 659 decrease in both, the electrostatic driving force for NP 660 absorption and the osmotic repulsion, and eventually 661 suppresses the globule absorption by PE brush (as seen in 662 Figure 9b). The combined effects of the NP volume-to-charge 663 ratio ω and salt concentration c_s are illustrated also by cross 664 sections of the 2D profiles of the insertion free energy curves, 665 $\Delta F(z, c_s)$ and $\Delta F(z, \omega)$, presented in Figure 10a and b, 666 respectively. Remarkably, an increase in ω or/and in salt 667 concentration c_s leads to the decrease in depth of the minimum 668 in $\Delta F(z)$ (and, eventually, its disappearance), but does not 669 affect its position at z = 0.

As it follows from our analysis, only small protein globules with large number of ionizable groups are efficiently absorbed by PE brushes at $\Delta pH_b \ge 0$, while bigger ones are not (unless other driving forces are involved).

We now examine the interplay between forces of electro-674 675 static attraction and osmotic repulsion in the case $\Delta p H_b \leq 0$, 676 i.e., when $Q(z) \ge 0$ at any $z \ge 0$. The free energy profiles 677 $\Delta F(z)$ corresponding to progressively increasing values of ω 678 are presented in Figure 11a and Figure 12a. They demonstrate 679 qualitatively new trends compared to the case $\Delta p H_h \geq 0$. For 680 example, at $\omega = 15$ the ionic contribution to the free energy 681 dominates, $\Delta F(z) \leq 0$ at any z, and thermodynamically most 682 favorable position of the globule is close to the grafting surface. 683 An increase in ω leads to the shift of the whole $\Delta F(z)$ curve 684 upward and change in its shape: The repulsive osmotic 685 contribution becomes dominant close to the grafting surface, 686 so that $\Delta F(z = 0)$ becomes positive, and a potential well 687 develops at the periphery of the brush where the negative ionic 688 contribution $\Delta F_{ion}(z)$ < 0 dominates over the osmotic 689 repulsion. The width and the depth of the potential well 690 decrease upon an increase in ω_{i} and its position is shifted to 691 the edge of the brush. Eventually, at large ω the peripheral 692 potential well disappears, and $\Delta F(z)$ becomes a monotonously $_{693}$ decreasing function of z, indicating expulsion of globules from 694 PE brush.

Another trend is observed at $\Delta pH_b \leq 0$ if ω is small and 696 kept constant, but the salt concentration increases, Figures 11b 697 and 12b: Notably the magnitudes of both electrostatic 698 (negative) and osmotic (positive) contributions to the free 699 energy diminish upon an increase in salt concentration C_s . At 700 very low salt concentration the electrostatic attraction 701 dominates over osmotic repulsion at any distance from the 702 surface and $\Delta F(z)$ is a monotonously increasing function of z. 703 At higher salt concentrations, the osmotic (repulsive) part of 704 the free energy starts to dominate in the proximal to the 705 grafting surface region, while in the distal region ($z \approx H$) the 706 electrostatic attraction, $\Delta F_{ion}(z)$, provides the dominant



Figure 10. Cross sections of the 2D profiles of the total free energy curves $\Delta F(z, c_s) = \Delta F_{\rm ion}(z, c_s) + \Delta F_{\rm vol}(z, c_s)$ (a) and $\Delta F(z, \omega) = \Delta F_{\rm ion}(z, \omega) + \Delta F_{\rm vol}(z, \omega)$ (b), both normalized by N_{Σ} , for a set values of ω corresponding to different globule volume to the number of charges ratio (a) and different salt concentrations (b) (with the corresponding color code, as indicated at the curves). $s/a^2 = 100$. Colored circles in panels indicate points of vanishing free energy, $\Delta F(z, c_s) = 0$ and $\Delta F(z, \omega) = 0$.

contribution to $\Delta F(z)$. As a result, a minimum in $\Delta F(z)$ 707 develops in the distal region. The depth of this minimum 708 decreases and its position z_{\min} is shifted toward the grafting 709 surface upon an increase in salt concentration and a 710 concomitant decrease in the brush thickness *H*. Hence, when 711 the osmotic contribution to the free energy becomes 712 comparable to the ionic one due to sufficiently large globule 713 volume or high salt concentration, the insertion free energy 714

f11f12

f10



Figure 11. Total free energy curves $\Delta F(z) = \Delta F_{\rm ion}(z) + \Delta F_{\rm vol}(z)$ normalized by N_{Σ} , at different globule volume to the number of charges raio ω . $C_{\rm s} = 0.015$ (a) and at $\omega = 24.3$ and varied salt concentration (b). The brush boundary, z = H, is indicated by the arrows. Dashdot horizontal lines indicate $\Delta F(z) = 0$.

715 curves decrease from $\Delta F(z=0) \ge 0$ in the proximal to the 716 grafting surface region and pass through a minimum (with 717 $\Delta F(z=z_{\min}) \le 0$) localized in the distal region of the brush. 718 Solid lines in the diagram in Figure 5 correspond to the salt 719 concentration $C_{\rm s}^{(\max,\omega)}$ separating regimes $\Delta F(0) \le 0$ 720 (absorption) and $\Delta F(0) > 0$ (repulsion). As follows from 721 Figure 5, this boundary is systematically displaced toward 722 lower salt concentration when ω (the globule bulkiness) 723 increases.

4. CONCLUSIONS

724 In this paper we have applied the analytical self-consistent field 725 Poisson–Boltzmann approach to study thermodynamics of 726 interactions between planar PE brushes and globular proteins, 727 modeled as nanoparticles (NPs) comprising weak cationic and 728 anionic groups on their surfaces. The position-dependent 729 insertion free energy $\Delta F(z)$ and the net charge Q(z) of the NP 730 were calculated as a function of environmental conditions (pH 731 and salt concentration c_s in the buffer), numbers of cationic 732 and anionic ionizable groups on the NP surface, the NP 733 volume V, and grafting density σ of the brush-forming 734 polyelectrolyte chains.

735 The insertion free energy $\Delta F(z) = \Delta F_{ion}(z) + \Delta F_{vol}(z)$ 736 accounts for the position-dependent ionization contribution 737 $\Delta F_{ion}(z)$ of NP in the electrostatic field induced by a planar PE 738 brush, and for the work $\Delta F_{vol}(z)$ performed against excess 739 osmotic pressure of mobile ions. As long as the electrostatic 740 potential $\psi(z)$ induced by permanently charged ("quenched") 741 PE brush can be tuned by changing the ionic strength in the 742 solution, $\Delta F_{vol}(z)$ is controlled solely by the globule volume V 743 and the salt concentration c_s in the buffer. On the contrary, 744 $\Delta F_{ion}(z)$ can be expressed as a function of ionization degrees of 745 cationic, $\alpha_{+}(z)$ and anionic, $\alpha_{-}(z)$ groups that depend on both,



Figure 12. Cross sections of the 2D profiles of the total free energy curves $\Delta F(z, c_s) = \Delta F_{ion}(z, c_s) + \Delta F_{vol}(z, c_s)$ (a) and $\Delta F(z)(z, \omega) = \Delta F_{ion}(z, \omega) + \Delta F_{vol}(z, \omega)$ (b), both normalized by N_{Σ} for a set values of ω corresponding to different globule volume to the number of charges ratio (a) and different salt concentrations (b), respectively (with the corresponding color code, as indicated at the curves). $s/a^2 = 100$. Colored circles in panels indicate points of vanishing free energy, $\Delta F(z, c_s) = 0$ and $\Delta F(z, \omega) = 0$.

the buffer pH_b, and the ionic strength (via $\psi(z)$). Importantly, 746 $\alpha_{-}(z)$ decreases providing positive contribution to $\Delta F_{ion}(z)$, 747 whereas $\alpha_{+}(z)$ increases providing negative contribution to 748 $\Delta F_{ion}(z)$ upon insertion of NP in polyanionic brush (with the 749 electrostatic potential $\psi(z) \leq 0$ monotonously increasing as a 750 function of z). Generalization to the case of polycationic PE 751 brush is straightforward by changing sign of $\psi(z)$ from negative 752 to positive.

⁷⁵⁴ In calculating the insertion free energy $\Delta F(z)$ we ⁷⁵⁵ implemented a number of approximations:

(i) An uptake of NPs (protein globules) from buffer 756 solution by PE brush is presumed to occur without 757 changing the conformational state of the globule and 758 spatial distribution of electrostatic potential $\psi(z)$ 759 induced by the brush. That is, NPs are considered as 760 probes. This approximation is valid at small protein 761 concentrations $c_b^{(\text{globules})}$ in buffer solution, and at no 762 strong binding of NPs to the brush-forming PE chains. 763

(ii) Small values of $c_b^{(\text{globules})} \ll 1$ allow us to specify the density profiles $c^{(\text{globules})}(z)$ of absorbed in the brush globules as

$$c^{\text{(globules)}}(z) = c_b^{\text{(globules)}} \exp[-\Delta F(z)]$$
(32)

₇₆₈ and the related partition coefficient,

767

769

$$\frac{\langle c^{\text{(globules)}} \rangle}{c_b^{\text{(globules)}}} = \frac{1}{H} \int_0^H \exp[-\Delta F(z)] dz$$
(33)

The latter specifies the ratio of average concentration 770 $\langle c^{(\text{globules})} \rangle$ of globules inside the brush, and concentration $c_b^{(\text{globules})}$ in the buffer solution. The limitation 771 772 $c_b^{(\text{globules})} \ll 1$ is most important at $pH_b \leq pH_{\text{IEP}}$ when 773 absorption of large amounts of NPs by colloidal 774 polyelectrolyte brushes unavoidably leads to collapse of 775 the brush and loss of colloid stability. This restriction is 776 less important if PE chains are grafted to planar 777 substrates, although perturbation of the PE brush 778 structure upon absorption of large amounts of NPs 779 also brings the theory to the limit of its validity. 780

- 781(iii) Reionization upon insertion is assumed to occur for all782 N_{Σ} ionizable groups on NP. However, for globular783proteins with compact ternary structure, only amino acid784residues localized at the globule-water interlace are785involved in (re)ionization process, leading therefore to786concomitant renormalization of N_{Σ} .
- Our approach does not account for additional attraction (iv) 787 between NP and PE brush due to charge-charge 788 correlations that provide negative contribution to the 789 insertion free energy $\Delta F(z)$. The charge-charge 790 correlations are most important for protein globules 791 with pronounced nonuniform ("patchy") distribution of 792 cationic and anionic groups on the globule surface. In 793 794 the latter case, the brush-forming PE chains may adsorb on the oppositely charged patches of charge, but be 795 depleted from similarly charged patches.²⁴ 796

(v) Our model neglects also the short-range nonelectrostatic 797 interactions between the brush-forming PE chains and 798 the surface of NPs that could be mediated by the solvent 799 quality or temperature. In spite of the anticipated 800 dominant role of electrostatic forces, such interactions 801 should be necessarily taken into account for full 802 quantitative prediction of absorption threshold and 803 diffusion rates for specific proteins. 804

By implementing the above approximations, and using the so6 self-consistent Poisson–Boltzmann approach, we have demso7 onstrated that the insertion free energy profiles $\Delta F(z)$ exhibit so8 complex patterns as a function of z depending on the environmental conditions (pH_b, c_s) and the globule volume s10 V normalized by the number of ionizable groups N_{Σ}. The s11 depth of the minima and the height of the maxima in $\Delta F(z)$ profiles are mediated by the number N_{Σ} of ionizable groups, ⁸¹² and the globule volume V. Notably, the implemented approach ⁸¹³ allows us to specify the lower pH_b boundary for uptake of NPs ⁸¹⁴ by PE brush. ⁸¹⁵

The analysis of our results indicates that one can distinguish $_{816}$ three characteristic ranges of pH_b with respect to the NP $_{817}$ isoelectric point, pH_{IEP}, in the buffer: $_{818}$

 $pH_b > pH_{IEP}$. The NP is strongly negatively charged in the 819 buffer, $Q_b < 0$. The NP charge Q remains negative upon 820 insertion in polyanionic brush, but decreases in magnitude 821 upon approach to the grafting surface, where the electrostatic 822 potential of PE brush is the strongest. The $\Delta F_{ion}(z)$ and $\Delta F(z)$ 823 are monotonously decreasing functions of z indicating 824 expulsion of NPs from the brush. The magnitude of the 825 repulsive free energy grows as a function of pH_b (due to the 826 increase in $|Q_b|$), but decreases upon an increase in the ionic 827 strength in the buffer solution. 828

 $\mathbf{pH}_b \geq \mathbf{pH}_{IEP}$. The NP is charged negatively in the buffer, 829 $Q_b \leq 0$, but acquires positive net charge upon insertion (or 830 approach to PE brush). The charge inversion, Q(z) = 0, occurs 831 at $z = z^*$ at which $\Delta F_{ion}(z)$ passes through a maximum. At 832 $z \leq z^*$ the globule charge becomes positive and keeps 833 increasing whereas the ionic part of the free energy, $\Delta F_{ion}(z)$, 834 decreases reaching either positive or negative value at the 835 grafting surface, z = 0. For small globules, $\Delta F(0) < 0$ indicates 836 their accumulation in the brush. At $\Delta F(0) > 0$, the local 837 minimum in $\Delta F_{ion}(z)$ at the grafting surface, z = 0, 838 corresponds to a metastable state separated by the potential 839 barrier from the bulk of the solution. Hence, even when the 840 NP net charge changes its sign from negative to positive, 841 absorption of NPs by PE brush is not necessarily 842 thermodynamically favorable though NPs may be kinetically 843 trapped there. 844

An increase in the ionic strength of the solution weakens the 845 electrostatic potential $\psi(z)$ and hinders reionization of anionic 846 and cationic groups of the inserted in the brush NP. As a result, 847 the charge inversion point, z^* , and the corresponding 848 maximum in $F_{ion}(z)$ are displaced toward the grafting surface 849 (where the magnitude of $\psi(z)$ is larger), the free energy 850 $\Delta F_{ion}(z = 0)$ grows and turns from negative to positive 851 indicating passing the absorption threshold. Eventually, at high 852 salt concentrations the potential $\psi(z)$ becomes too weak to 853 induce reionization of the NP inside the brush, and the NPs 854 are repelled by the brush. 855

A progressive increase in the NP volume V (an increase in 856 ω) at constant ionic strength leads to the growth of repulsive 857 osmotic contribution $\Delta F_{\rm vol}(z)$ at constant $\Delta F_{\rm ion}(z)$. As a result, 858 the $\Delta F(z)$ curves are shifted upward while the position of 859 maximum, $z_{\rm max}$, is displaced toward the grafting surface. 860 Importantly, now the position of maximum, $z_{\rm max}$, does not 861 coincide with the charge inversion point, z^* , and 862 $Q(z = z_{\rm max}) \ge 0$. Further increase in the NP volume V leads 863 to $\Delta F(z = 0) \ge 0$ and eventual transformation of $\Delta F(z)$ into 864 monotonously decreasing curve. That is, expulsion of the bulky 865 globule from the brush in spite of the charge inversion (which 866 can be traced in the $\Delta F_{\rm ion}(z)$ and Q(z) curves). 867

 $\mathbf{pH}_b \leq \mathbf{pH}_{\text{IEP}}$. The NP is positively charged in the buffer 868 and, therefore, attracted to the PE brush by the Coulomb 869 force. The $\Delta F_{\text{ion}}(z) \leq 0$ at all z, and the NP positive charge 870 grows upon insertion into the brush and approach to the 871 grafting surface. However, absorption of a bulky globule can be 872 hindered and even fully suppressed due to osmotic (repulsive) 873 term, $\Delta F_{\text{vol}}(z)$. An increase in the globule volume (and in 874

875 $\Delta F_{\rm vol}(z)$ at constant salt concentration $c_{\rm s}$ leads to the increase 876 in $\Delta F(z)$ primarily in the proximal to the grafting surface 877 region, flattening of the presurface potential well, and eventually leading to the appearance of the presurface 879 maximum with $\Delta F(z=0) \geq 0$. The maximum is separated 880 from the bulk of the solution by the minimum which progressively gets more shallow and narrow, and is displaced 881 882 to the external boundary of PE brush. A similar evolution of $\Delta F(z)$ curve is observed for globules with fixed V and N_{Σ} upon 883 variations in the salt concentration. The minimum in $\Delta F(z)$ is 884 885 shifted toward the periphery of the brush (and progressively disappears) upon an increase in c_s . The theory thereby predicts 886 that below IEP the interplay between ionic attraction and 887 osmotic repulsion may result in preferential accumulation of 888 the absorbed protein globules in the central or even peripheral 889 regions of the brush, whereas the proximal to the grafting 890 surface region is depleted from globules. This feature is most 891 892 attractive in design of bionanoreactors in which accumulation 893 of the proteins (enzymes) in the brush is required, but their direct contacts with underlying substrate (that could lead to 894 895 nonspecific adsorption, denaturation, and loss of enzymatic activity) should be avoided. 896

We remark that amplitudes of the minima and maxima in 897 898 $\Delta F(z)$ curves that determine the thermodynamic stability of 899 the protein absorbed state or the probability of overcoming the 900 potential barrier separating the absorbed state from the bulk of 901 the solution or from the grafting surface depend on the 902 number of charged groups and volume of the globule. With 903 typical values of $N_{\Sigma} \sim 10^2$, the potential well easily reaches the 904 depth of a few $k_{\rm B}T$ under experimentally relevant conditions. 905 Furthermore, reionization and the NP absorption on the wrong side" of the IEP is suppressed by increasing salt 906 concentration (in full agreement with the experimental data²⁰), 907 but might be operational for sufficiently densely grafted PE 908 brushes that induce strong local electrostatic field. 909

To summarize, our theory predicts how the electrostatic and 910 911 osmotic parts of the insertion free energy change upon 912 insertion of ampholytic NP containing pH-sensitive acidic and 913 basic groups in a planar PE brush from the solution in a wide $_{914}$ range of the buffer pH_b. On the "wrong side" of the isoelectric 915 point, the negative balance in the free energy may be assured 916 by overcompensation of the free energy losses due to 917 suppression of ionization of similarly (with respect to the 918 brush) charged monomeric groups by gains due to enhanced 919 ionization of the oppositely charged ones, and be accompanied 920 by the change in the sign of the net charge of NP inside the 921 brush. However, the local minimum in the NP free energy 922 inside the brush may correspond to a metastable state even if it 923 is accompanied by the net charge reversal. Importantly, 924 knowledge of the insertion free energy profile $\Delta F(z)$ allows 925 also for the calculation and control of the diffusion rates of 926 NPs through the brush to be considered in our forthcoming 927 publication.

928 ASSOCIATED CONTENT

929 **Supporting Information**

930 The Supporting Information is available free of charge at 931 https://pubs.acs.org/doi/10.1021/acs.biomac.2c01153.

Detailed derivation of the electrostatic potential
distribution in the planar PE brush (PDF)

960

A	UTHOR INFORMATION	934	
Corres	sponding Author	935	
Ole	Oleg V. Borisov – CNRS, Université de Pau et des Pays de		
ľ	Adour UMR 5254, Institut des Sciences Analytiques et de	937	
P_{i}	hysico-Chimie pour l'Environnement et les Matériaux,	938	
64	4053 Pau, France; St. Petersburg National Research	939	
U	niversity of Information Technologies, Mechanics and	940	
0	ptics, 197101 St. Petersburg, Russia; Institute of	941	
$N_{\rm c}$	lacromolecular Compounds of the Russian Academy of	942	
Se	ciences, 199004 St. Petersburg, Russia; 💿 orcid.org/0000-	943	
00	002-9281-9093; Email: oleg.borisov@univ-pau.fr	944	
Autho	ors	945	
Tati	Tatiana O. Salamatova – St. Petersburg National Research		
U	niversity of Information Technologies, Mechanics and	947	
0	ptics, 197101 St. Petersburg, Russia; 💿 orcid.org/0000-	948	
00	002-7559-1824	949	
Mik	chail Y. Laktionov – St. Petersburg National Research	950	
U	Iniversity of Information Technologies, Mechanics and	951	
0	ptics, 197101 St. Petersburg, Russia	952	
Eka	terina B. Zhulina – Institute of Macromolecular	953	
С	ompounds of the Russian Academy of Sciences, 199004 St.	954	
P_{i}	etersburg, Russia; 💿 orcid.org/0000-0001-9139-3484	955	
Comp	lete contact information is available at:	956	
https:/	//pubs.acs.org/10.1021/acs.biomac.2c01153	957	
Notes		958	
The a	uthors declare no competing financial interest.	959	

ACKNOWLEDGMENTS

This work was financially supported by Russian Foundation for 961 Basic Research, Grant 21-53-10005. 962

REFERENCES	963

(1) Achazi, K.; Haag, R.; Ballauff, M.; Dernedde, J.; Kizhakkedathu, 964 J. N.; Maysinger, D.; Multhaup, G. Understanding the Interaction of 965 Polyelectrolyte Architectures with Proteins and Biosystems. *Angew.* 966 *Chem., Int. Ed.* **2021**, 60 (8), 3882–3904. 967

(2) Nie, C. A. X.; Pouyan, P.; Lauster, D.; Trimpert, J.; Kerkhoff, Y.; 968 Szekeres, G. P.; Wallert, M.; Block, S.; Sahoo, A. K.; Dernedde, J.; 969 Pagel, K.; Kaufer, B. B.; Netz, R. R.; Ballauff, M.; Haag, R. Polysulfates 970 Block SARS-CoV-2 Uptake through Electrostatic Interactions. *Angew.* 971 *Chem., Int. Ed.* **2021**, 60 (29), 15870–15878. 972

(3) Kapelner, R. A.; Yeong, V.; Obermeyer, A. C. Molecular 973 determinants of protein-based coacervates. *Curr. Opin. Colloid* 974 *Interface Sci.* 2021, *52*, 101407. 975

(4) Yeong, V.; Werth, E. G.; Brown, L. M.; Obermeyer, A. C. 976 Formation of biomolecular condensates in bacteria by tuning protein 977 electrostatics. *ACS Cent. Sci.* **2020**, *6*, 2301–2310. 978

(5) Kabanov, A. V.; Kabanov, V. A. Interpolyelectrolyte and block 979 ionomer complexes for gene delivery: physico-chemical aspects. *Adv.* 980 *Drug Delivery Rev.* **1998**, 30 (1–3), 49–60. 981

(6) Schallon, A.; Synatschke, C. V.; Jerome, V.; Müller, A. H. E.; 982 Freitag, R. Nanopartiulate Nonviral Agent for the Effective Delivery of 983 pDNA and si RNA to Differentiated Cells and Primary Human T 984 Lymphocytes. *Biomacromolecules* **2012**, *13*, 3463–3474. 985

(7) Miyata, K.; Nishiyama, N.; Kataoka, K. Rational design of smart 986 supramolecular assemblies for gene delivery: chemical challenges in 987 the creation of artificial viruses. *Chem.Soc. Rev.* **2012**, *41*, 2562–2574. 988 (8) Yu, T.; Liu, X.; Bolcato-Bellemin, A.-L.; Wang, Y.; Liu, C.; 989 Erbacher, P.; Qu, F.; Rocchi, P.; Behr, J.-P.; Peng, L. An amphiphilic 990 dendrimer for effective delivery of small interfering RNA and gene 991 silencing in vitro and in vivo. *Angew. Chem., Int. Ed.* **2012**, *124*, 8606–992 8612. 993 994 (9) Liu, X.; Zhou, J.; Yu, T.; Chen, C.; Cheng, Q.; Sengupta, K.;
995 Huang, Y.; Li, H.; Liu, C.; Wang, Y.; Posocco, P.; Wang, M.; Cui, Q.;
996 Giorgio, S.; Fermeglia, M.; Qu, F.; Pricl, S.; Shi, Y.; Liang, Z.; Rocchi,
997 P.; Rossi, J. J.; Peng, L. Adaptive Amphiphilic Dendrimer-Based
998 Nanoassemblies as Robust and Versatile siRNA Delivery Systems.
999 Angew. Chem., Int. Ed. 2014, 126, 12016–12021.

1000 (10) Fan, X.; Zhao, Y.; Xu, W.; Li, L. Linear-Dendritic Block 1001 Copolymer for Drug and Gene Delivery. *Mater. Sci. Eng., C* 2016, *62*, 1002 943–959.

1003 (11) Malmsten, M.; Bysell, H.; Hansson, P. Biomacromolecules in 1004 Microgels - Opportunities and Challenges for Drug Delivery. *Curr.* 1005 *Opin. Colloid Interface Sci.* **2010**, *15*, 435–444.

1006 (12) Bysell, H.; Mansson, R.; Hansson, P.; Malmsten, M. Microgels 1007 and Microcapsules in Peptide and Protein Drug Delivery. *Adv. Drug* 1008 *Delivery Rev.* **2011**, *63*, 1172–1185.

1009 (13) Hachim, D.; Whittaker, T. E.; Kim, H.; Stevens, M. M. 1010 Glycosaminoglycan-based biomaterials for growth factor and cytokine 1011 delivery: Making the right choices. *J. Controlled Release* **2019**, *313*, 1012 131–147.

1013 (14) Braatz, D.; Dimde, M.; Ma, G.; Zhong, Y.; Tully, M.; 1014 Grotzinger, C.; Zhang, Y.; Mavroskoufis, A.; Schirner, M.; Zhong, Z.; 1015 Ballauff, M.; Haag, R. Toolbox of Biodegradable Dendritic (Poly 1016 glycerol sulfate)-SS-poly(ester) Micelles for Cancer Treatment: 1017 Stability, Drug Release, and Tumor Targeting. *Biomacromolecules* 1018 **2021**, *22* (6), 2625–2640.

1019 (15) Kiani, C.; Chen, L.; Wu, Y. J.; Yee, A. J.; Yang, B. B. Structure 1020 and functions of aggrecan. *Cell Res.* **2002**, *12*, 19–32.

1021 (16) Cagno, V.; Tseligka, E. D.; Jones, S. T.; Tapparel, C. Heparan 1022 sulfate proteoglycans and viral attachment: True receptors or 1023 adaptation bias? *Viruses* **2019**, *11* (7), 596.

1024 (17) Wittemann, A.; Haupt, B.; Ballauff, M. Adsorption of proteins 1025 on spherical polyelectrolyte brushes in aqueous solution. *Phys. Chem.* 1026 *Chem. Phys.* **2003**, *5*, 1671–1677.

1027 (18) Wittemann, A.; Ballauff, M. Interaction of proteins with linear 1028 polyelectrolytes and spherical polyelectrolyte brushes in aqueous 1029 solution. *Phys. Chem. Chem. Phys.* **2006**, *8*, 5269–5275.

(19) Becker, A. L.; Henzler, K.; Welsch, N.; Ballauff, M.; Borisov, O.
1031 V. Proteins and polyelectrolytes: A charge relationship. *Curr. Opin.*1032 *Colloid Interface Sci.* 2012, *17*, 90–96.

1033 (20) Walkowiak, J.; Gradzielski, M.; Zauscher, S.; Ballauff, M. 1034 Interaction of Proteins with a Planar Poly(acrylic acid) Brush: 1035 Analysis by Quartz Crystal Microbalance with Dissipation Monitoring 1036 (QCM-D). *Polymers* **2021**, *13*, 122.

1037 (21) Yigit, C.; Welsch, N.; Ballauff, M.; Dzubiella, J. Protein 1038 Sorption to Charged Microgels: Characterizing Binding Isotherms 1039 and Driving Forces. *Langmuir* **2012**, *28*, 14373–14385.

1040 (22) Biesheuvel, P. M.; Wittemann, A. A modified box model 1041 including charged polyelectrolyte brush: self-consistent field theory. 1042 J.Phys.Chem. B **2005**, 109, 4209–4214.

1043 (23) de Vos, W. M.; Leermakers, F. A. M.; de Keizer, A.; Cohen 1044 Stuart, M. A.; Kleijn, J. M. Field theoretical analysis of driving forces 1045 for the uptake of proteins by like-charge polyelectrolyte brushes: 1046 effects of charge regulation and patchiness. *Langmuir* **2010**, *26*, 249– 1047 259.

1048 (24) Leermakers, F. A. M.; Ballauff, M.; Borisov, O. V. On the 1049 mechanisms of interaction of globular proteins with polyelectrolyte 1050 brushes. *Langmuir* **2007**, *23*, 237–247.

1051 (25) Xu, X.; Angioletti-Uberti, S.; Lu, Y.; Dzubiella, J.; Ballauff, M. 1052 Interaction of Proteins with Polyelectrolytes: Comparison of Theory 1053 to Experiment. *Langmuir* **2019**, *35*, 5373–5391.

1054 (26) Kim, S.; Sureka, H. V.; Kayitmazer, A. B.; Wang, G.; Swan, J. 1055 W.; Olsen, B. D. Effect of protein surface charge distribution on 1056 protein-polyelectrolyte complexation. *Biomacromolecules* **2020**, *21*, 1057 3026–3037.

1058 (27) Lunkad, R.; Barroso da Silva, F. L.; Kosovan, P. Both Charge-1059 Regulation and Charge-Patch Distribution Can Adsorption on the 1060 Wrong Side of the Isoelectric Point. *J. Am. Chem. Soc.* **2022**, 144, 1061 1813–1825. (28) Laktionov, M. Y.; Zhulina, E. B.; Borisov, O. V. Proteins and 1062 polyampholytes interacting with polyelectrolyte brushes and micro- 1063 gels: the charge reversal concept revised. *Langmuir* **2021**, 37, 2865– 1064 2873. 1065

(29) Zhulina, E. B.; Borisov, O. V. Structure and Interactions of 1066 Weakly Charged Polyelectrolyte Brushes: Self-Consistent Field 1067 Theory. *textit J. Chem. Phys.* **1997**, *107*, 5952–5967. 1068

(30) Zhulina, E. B.; Klein Wolterink, J.; Borisov, O. V. Screening 1069 Effects in Polyelectrolyte Brush: Self-Consistent Field Theory. 1070 *Macromolecules* **2000**, *33*, 4945–4953. 1071

(31) Lebedeva, I. O.; Zhulina, E. B.; Borisov, O. V. Self-consistent 1072 Field Theory of Polyelectrolyte Brushes with Finite Chain 1073 Extensibility. J. Chem. Phys. **2017**, 146, 214901–6. 1074

(32) Zhulina, E. B.; Borisov, O. V. Poisson-Boltzmann Theory of 1075 pH-Sensitive (Annealing) Polyelectrolyte Brush. *Langmuir* **2011**, 27, 1076 10615–10633.

(33) Zhulina, E. B.; Borisov, O. V. Brushes of Dendritically 1078 Branched Polyelectrolytes. *Macromolecules* **2015**, *48* (19), 1499–1079 1508. 1080

(34) Zhulina, E. B.; Boulakh, A. B.; Borisov, O. V. Repulsive Forces 1081 between Spherical Polyelectrolyte Brushes in Salt-Free Solution. Z. 1082 *Phys. Chem. (Berlin, Ger.)* **2012**, 226, 625–643. 1083

(35) Lunkad, R.; Murmiliuk, A.; Tosner, Z.; Stepanek, M.; Kosovan, 1084 P. Role of pKA in Charge Regulation and Conformation of Various 1085 Peptide Sequences. *Polymers* **2021**, *13*, 214. 1086

(36) Lunkad, R.; Biehl, P.; Murmiliuk, A.; Blanco, P. M.; Mons, P.; 1087 Stepanek, M.; Schacher, F. H.; Kosovan, P. Simulations and 1088 Potentiometric Titrations Enable Reliable Determination of Effective 1089 pK_a Values of Various Polyzwitterions. *Macromolecules* **2022**, *55*, 1090 7775–7784. 1091

(37) Halperin, A.; Kröger, M.; Zhulina, E. B. Colloid-brush 1092 interactions: The effect of solvent quality. *Macromolecules* **2011**, *44*, 1093 3622–3638. 1094

(38) Merlitz, H.; Wu, C.-X.; Sommer, J.-U. Inclusion Free Energy of 1095 Nanoparticles in Polymer Brushes. *Macromolecules* **2012**, *45*, 8494–1096 8501. 1097

(39) Laktionov, M. Y.; Shavykin, O. V.; Leermakers, F. A. M.; 1098 Zhulina, E. B.; Borisov, O. V. Colloidal particles interacting with a 1099 polymer brush: a self-consistent field theory. *Phys. Chem. Chem. Phys.* 1100 **2022**, 24, 8463–8476. 1101

(40) Landau, L. D.; Lifshitz, E. M. Statistical Physics; Pergamon 1102 Press: Oxford, 1986.

(41) RCSB PDB: Homepage. https://www.rcsb.org (accessed 1104 2022-08-21). 1105